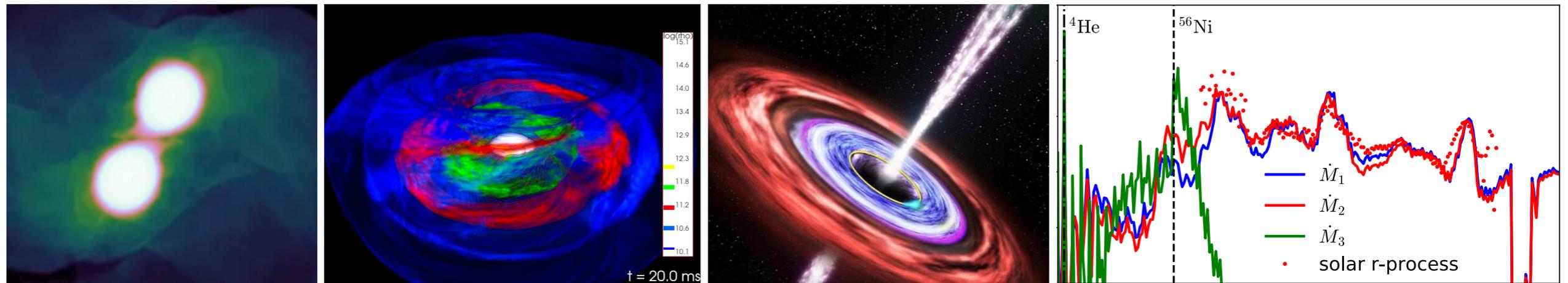


# Post-merger evolution and nucleosynthesis



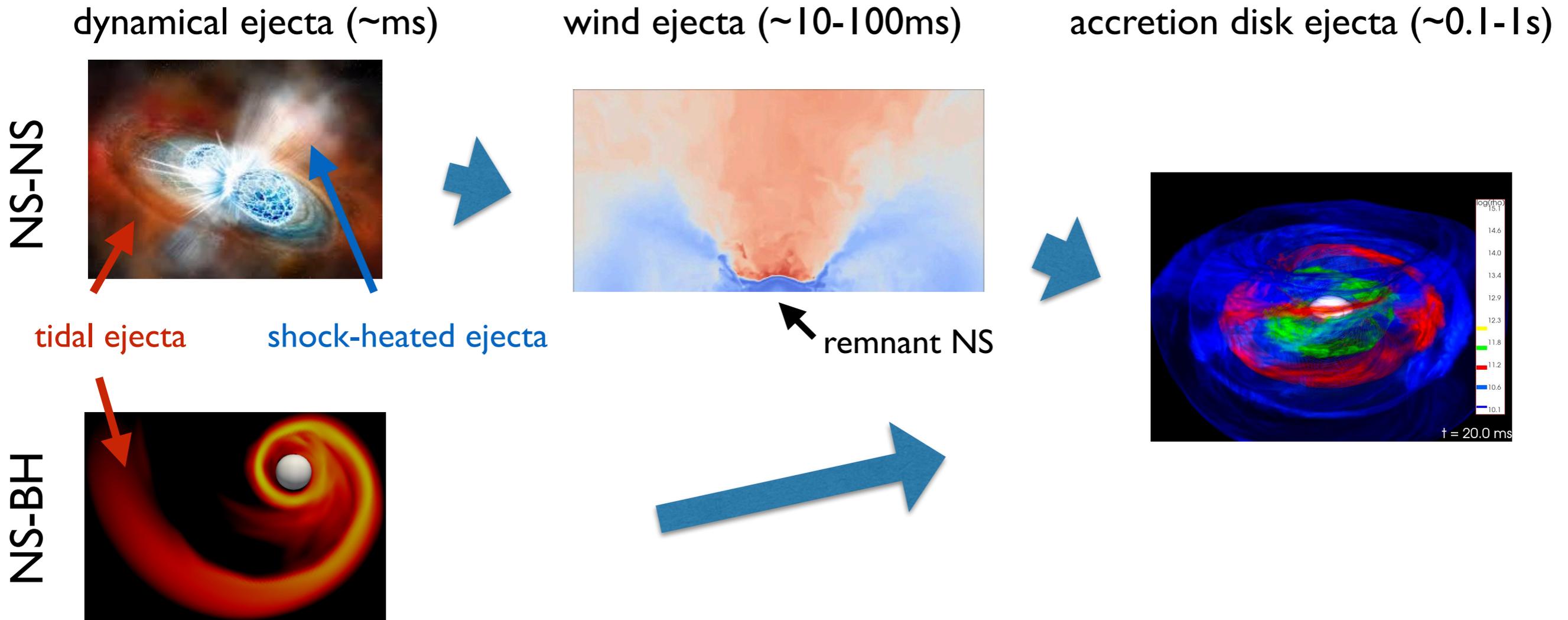
Daniel M. Siegel

*Perimeter Institute for Theoretical Physics  
and University of Guelph, Ontario, Canada*



TCAN meeting, July 12-15, 2021

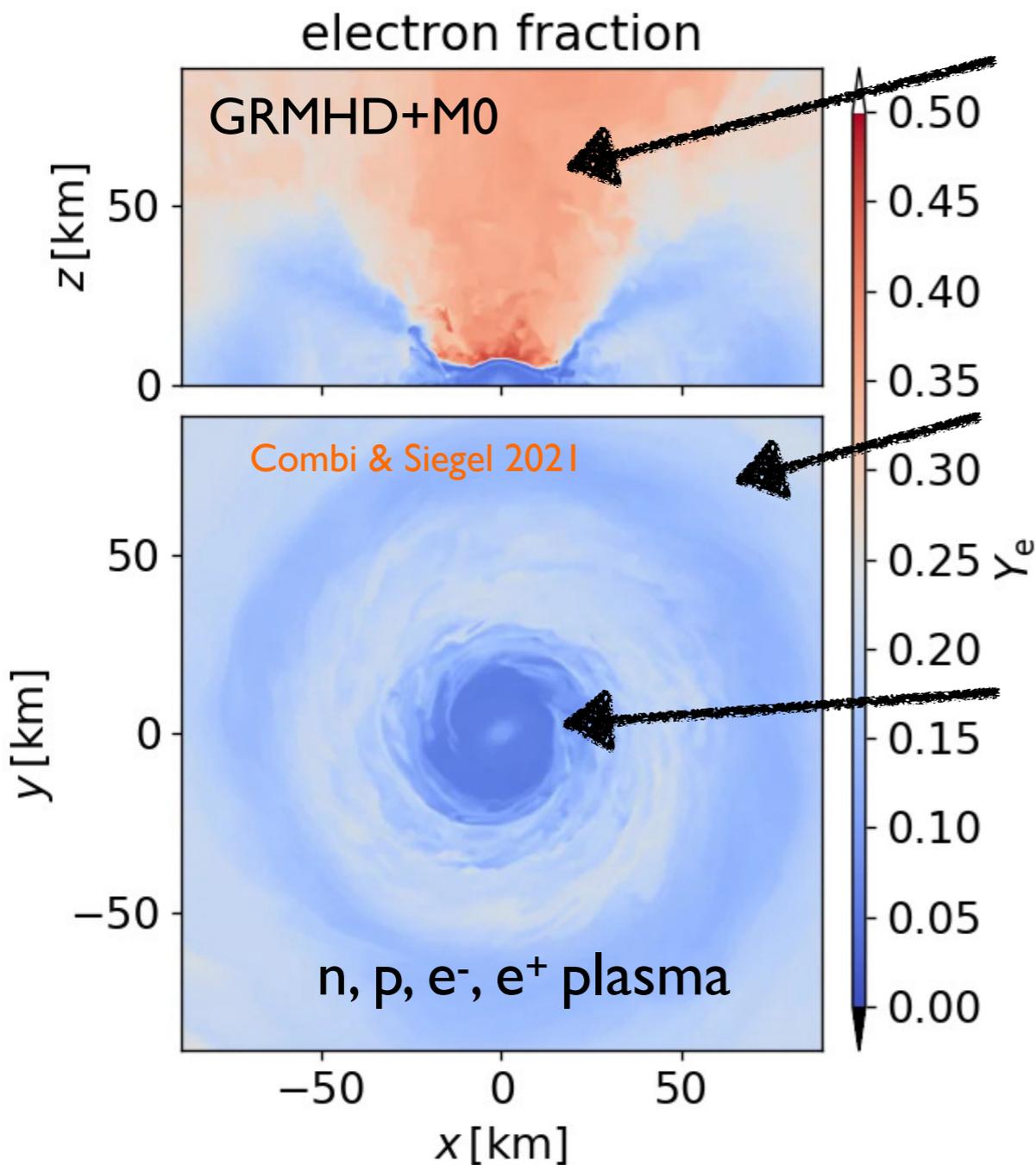
# Neutron-star mergers



Some complications for NS-NS:

- magnetically driven winds
- neutrino-driven winds
- GWs, non-linear (magneto-)hydrodynamics

# Early post-merger phase



neutrino irradiation changes plasma composition:  
**high proton fraction** ( $Y_e > 0.25$ ), hot wind ejecta

**medium proton fraction** ( $Y_e$ ), hot  
 (> 10 MeV) disk wind

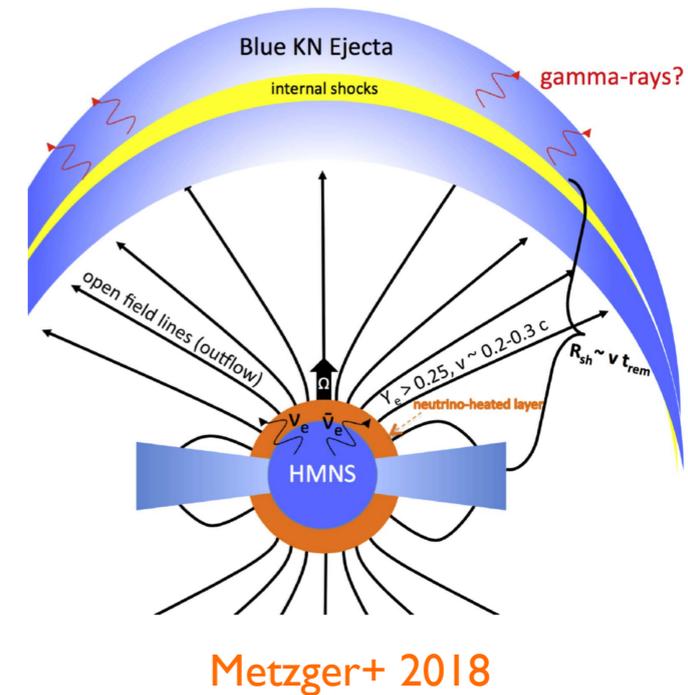
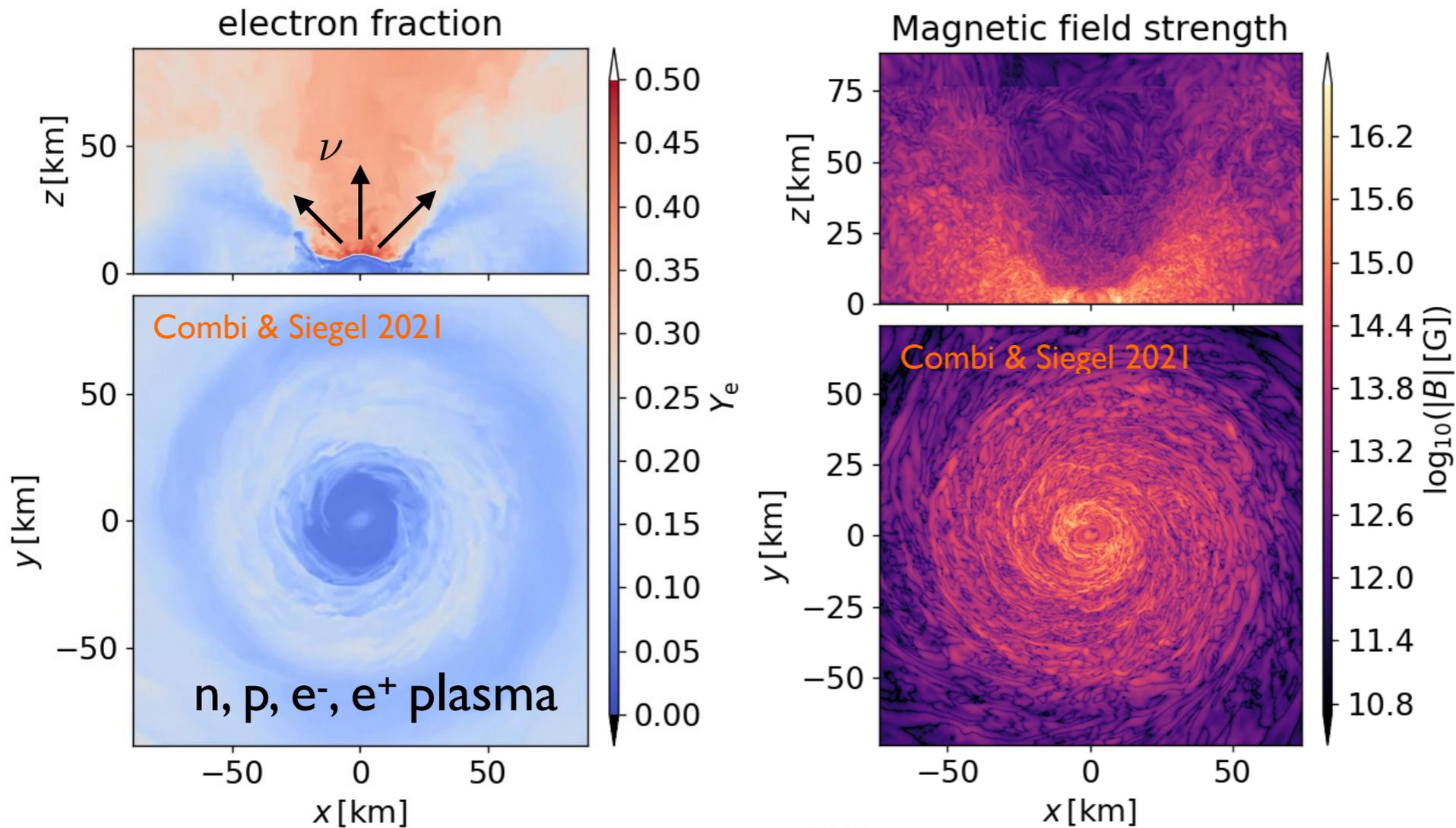
hot (> 30 MeV)  
**neutron star**

- neutrino-driven winds
- magnetically driven winds
- GWs, non-linear hydrodynamics

Dessart+ 2009  
 Siegel+ 2014  
 Ciolfi & Kalinani 2020  
 Metzger+ 2018  
 Nedora+ 2019, 2021  
 Kastaun & Ohme 2021  
 Shibata+ 2021

# Early post-merger phase

## Mass ejection: neutrino- and magnetically driven winds



- neutrino-driven winds
- magnetically driven winds
- GWs, non-linear hydrodynamics

Dessart+ 2009  
 Siegel+ 2014  
 Ciolfi & Kalinani 2020  
 Metzger+ 2018

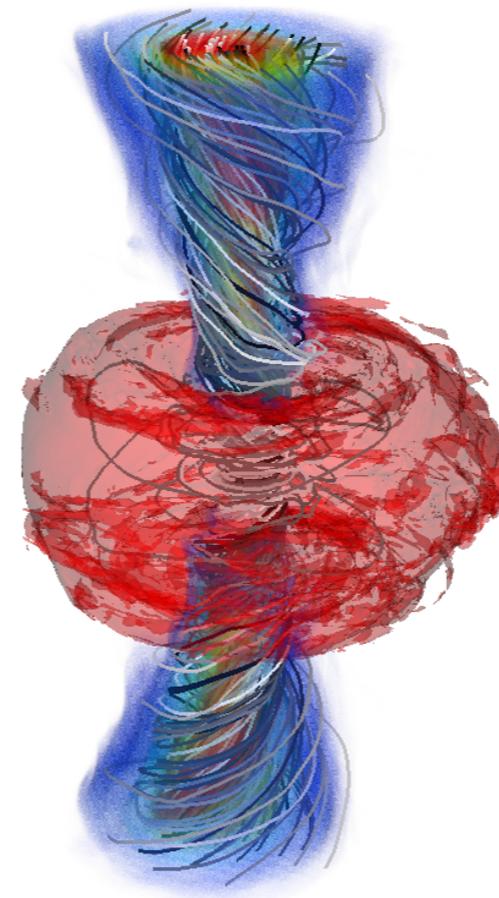
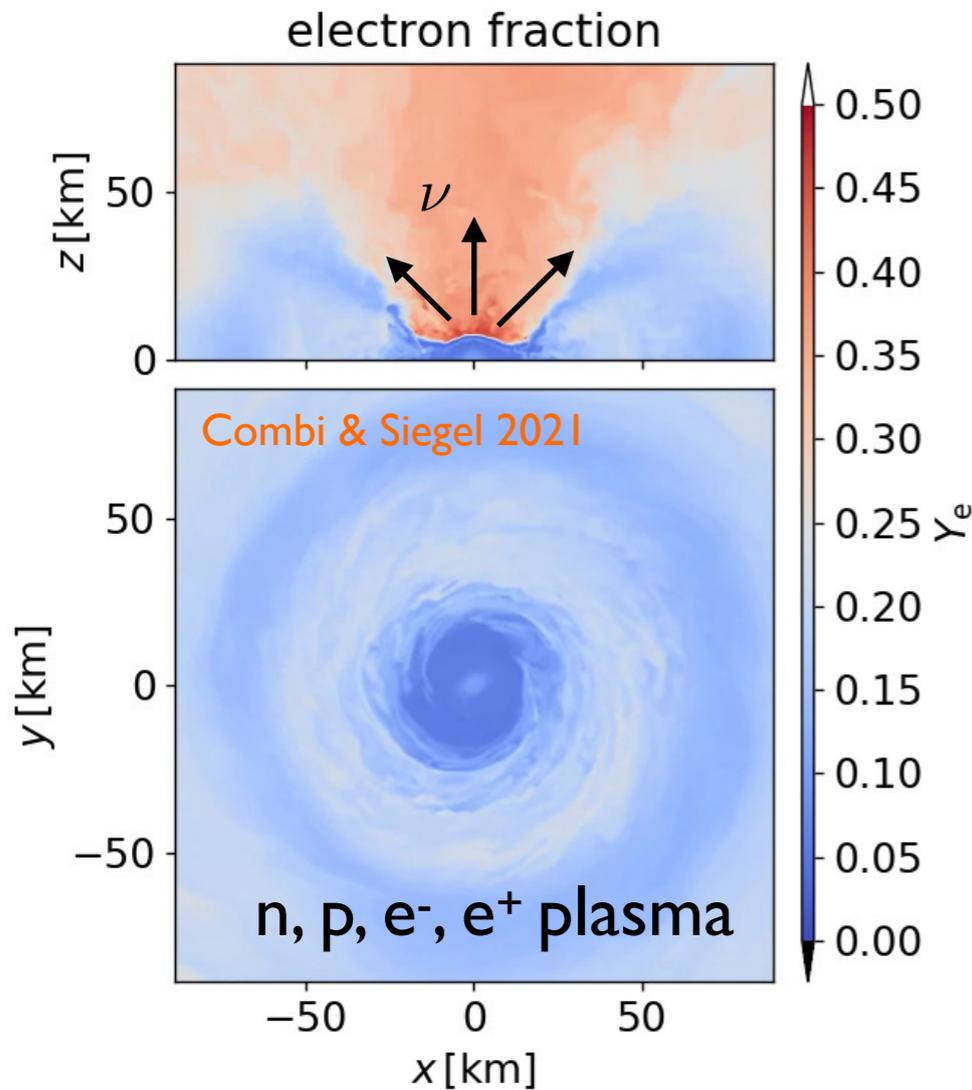
Nedora+ 2019, 2021  
 Kastaun & Ohme 2021  
 Shibata+ 2021

Estimated ejecta mass:

$$M_{ej} \sim (10^{-4} - 10^{-2}) M_{\odot} \left( \frac{t_{rem}}{0.1s} \right)$$

# Early post-merger phase

Mass ejection: neutrino- and magnetically driven winds



Start with  $10^{15}$ G poloidal B-field after merger, short lived remnant ( $\sim 20$ ms)

$$\dot{M} \sim 10^{-1} M_{\odot} \text{ s}^{-1}$$

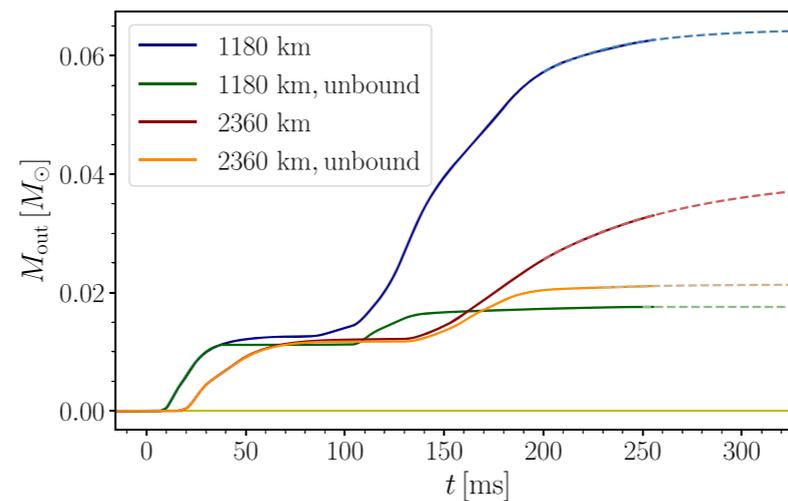
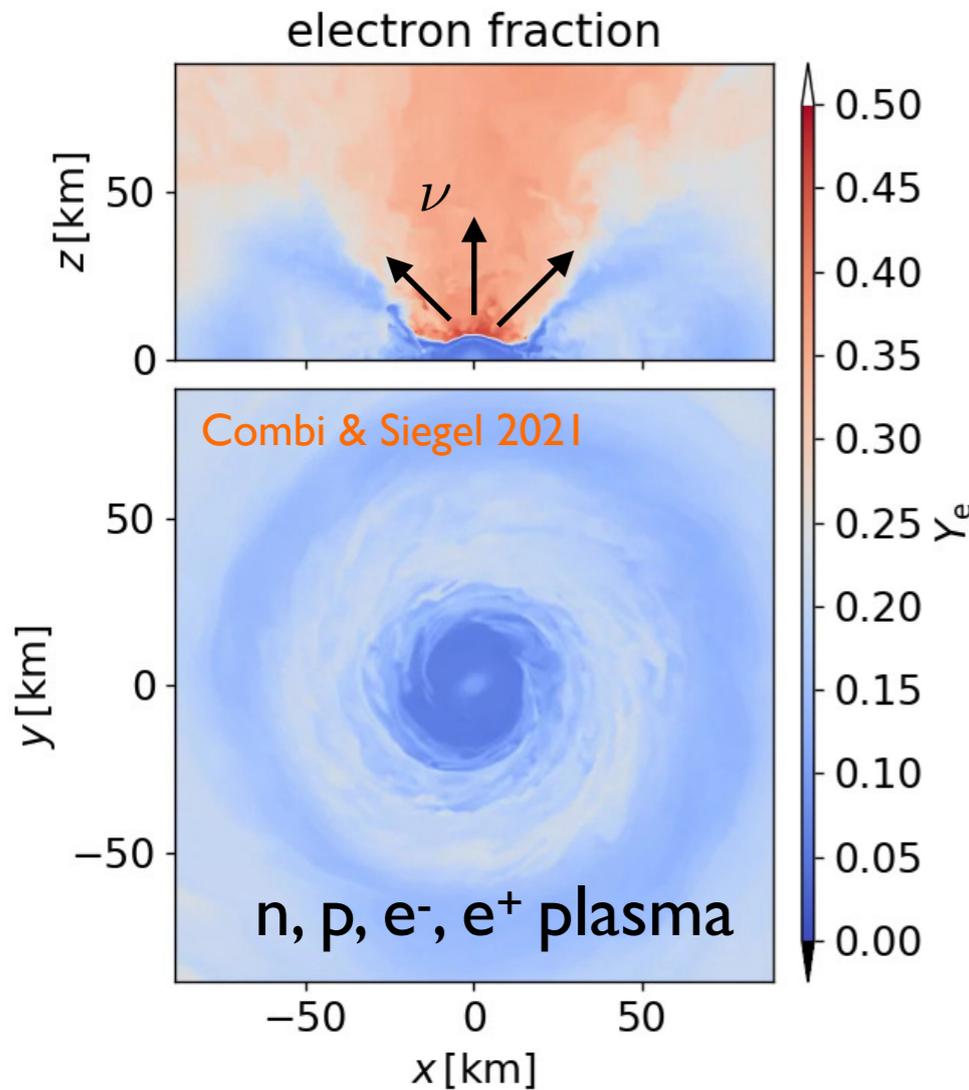
$$v \sim 0.05 - 0.4c$$

Mösta+ 2020

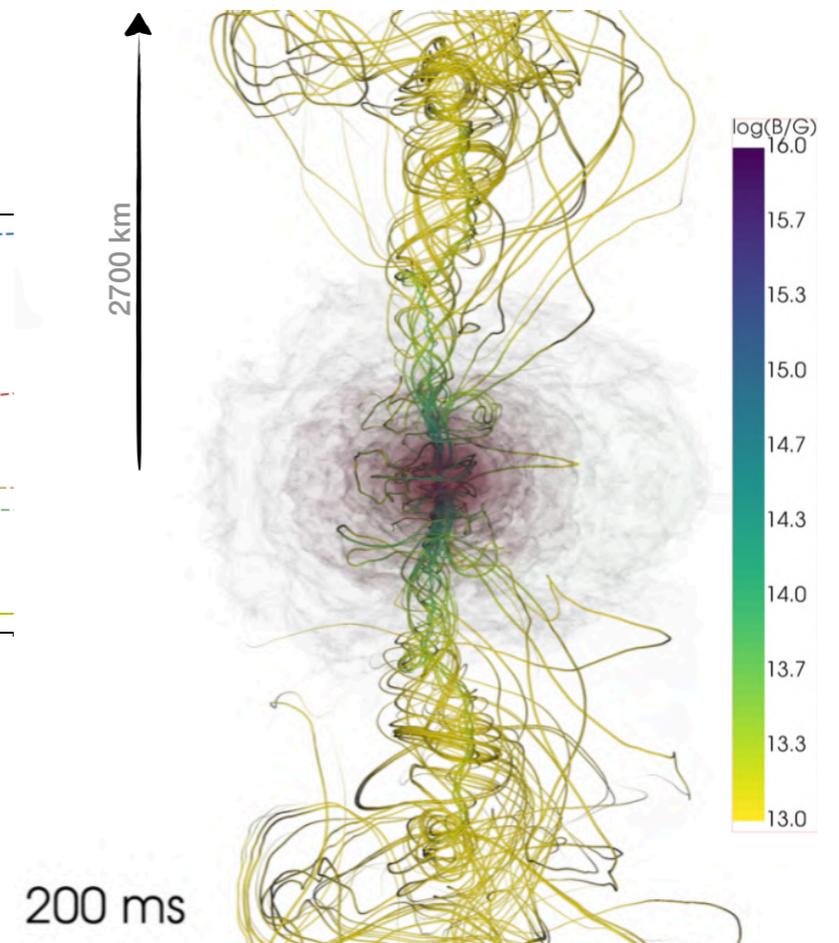
- neutrino-driven winds
  - magnetically driven winds
  - GWs, non-linear hydrodynamics
- Dessart+ 2009  
 Siegel+ 2014  
 Ciolfi & Kalinani 2020  
 Metzger+ 2018  
 Lehner+ 2016, Nedora+ 2019, 2021  
 Kastaun & Ohme 2021  
 Shibata+ 2021

# Early post-merger phase

Mass ejection: neutrino- and magnetically driven winds



Cioffi & Kalinani 2020



- neutrino-driven winds
- magnetically driven winds
- GWs, non-linear hydrodynamics

Dessart+ 2009

Siegel+ 2014

Cioffi & Kalinani 2020

Metzger+ 2018

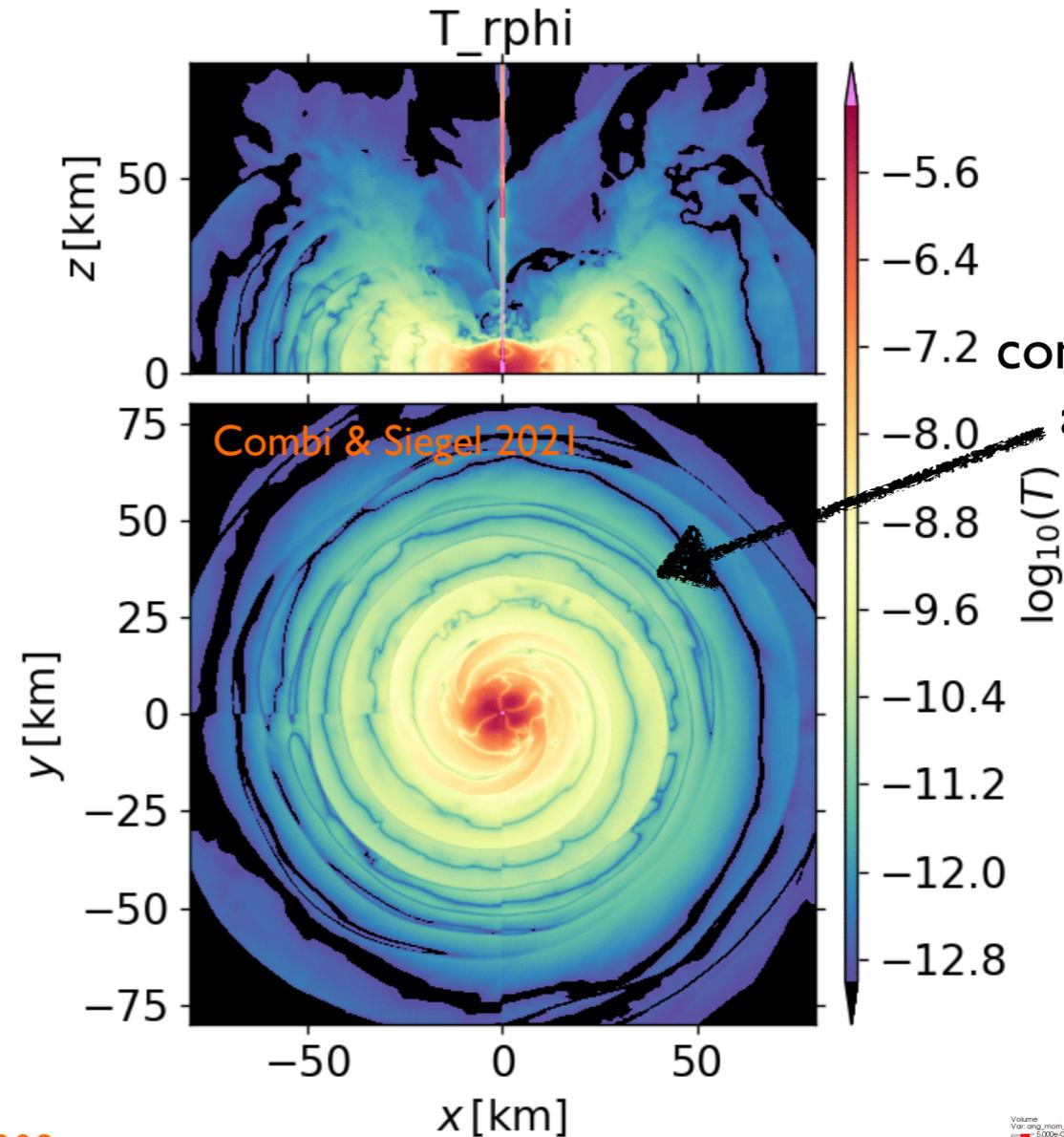
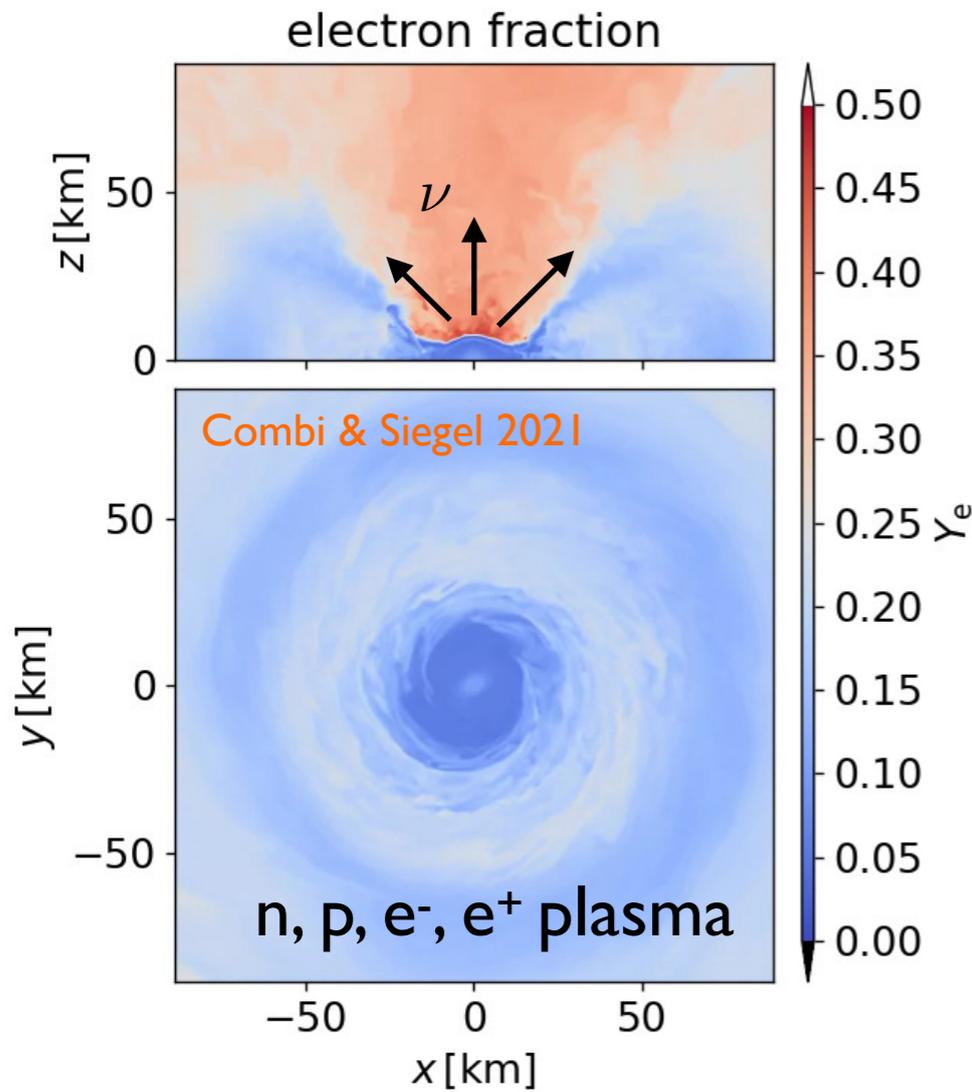
Lehner+ 2016, Nedora+ 2019, 2021

Kastaun & Ohme 2021

Shibata+ 2021

# Early post-merger phase

Mass ejection: disk winds & spiral waves

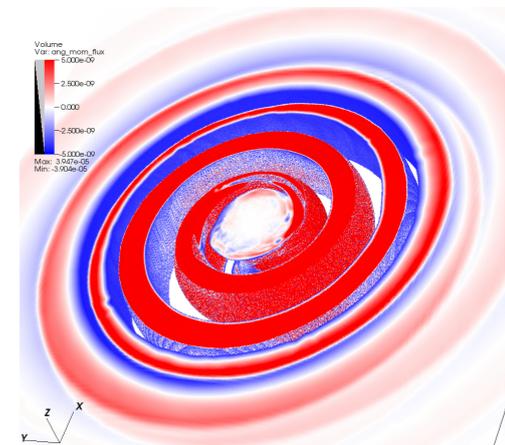
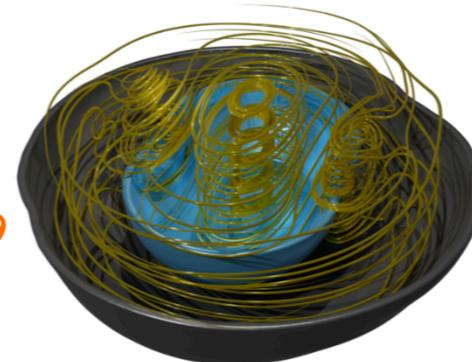


competition btw. MRI and spiral waves

- neutrino-driven winds
- magnetically driven winds
- GWs, non-linear hydrodynamics

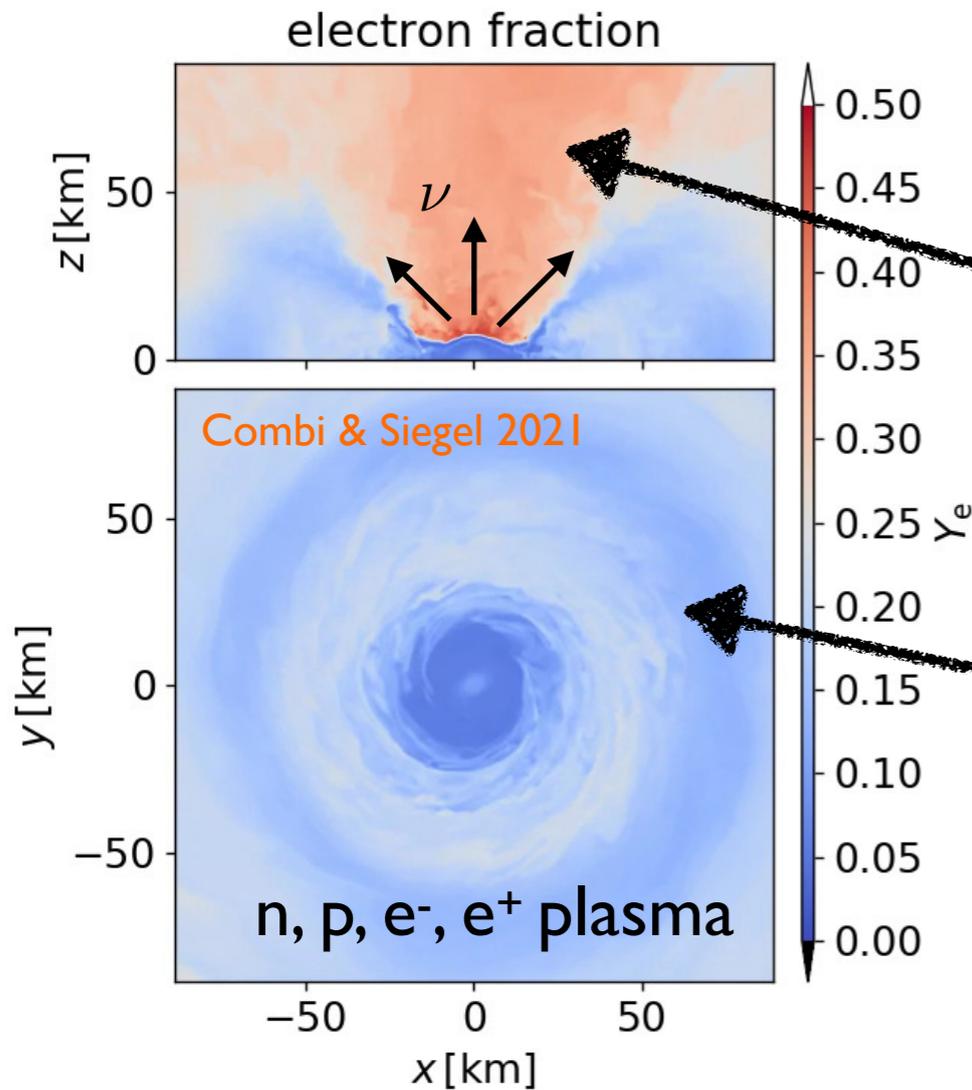
Dessart+ 2009  
 Siegel+ 2014  
 Ciolfi & Kalinani 2020  
 Metzger+ 2018

Lehner+ 2016. Nedora+ 2019  
 Kastaun & Ohme 2021  
 Shibata+ 2021



# Early post-merger phase

## Mass ejection: composition



Chiefly determined by:  $e^- + p \leftrightarrow n + \nu_e$   
(radiation transport!)  $e^+ + n \leftrightarrow p + \bar{\nu}_e$

absorption dominated, non-degenerate: [Qian & Woosley 1996](#)

$$Y_e^{\text{eq}} \simeq \left[ 1 + \frac{L_{\bar{\nu}_e} \epsilon_{\bar{\nu}_e} - 2\Delta + 1.2\Delta^2/\epsilon_{\bar{\nu}_e}}{L_{\nu_e} \epsilon_{\nu_e} + 2\Delta + 1.2\Delta^2/\epsilon_{\nu_e}} \right]^{-1} \sim 0.4 - 0.5$$

absorption and emission important, degenerate

→ typically low  $Y_e$ :  $Y_e \simeq Y_e^{\text{eq}} \sim 0.1 - 0.2$  [Beloborodov 2001](#)

final  $Y_e$  of **disk outflow** strongly depends on ejection path and timescale as it traverses different regimes (details of accretion disk evolution matter):

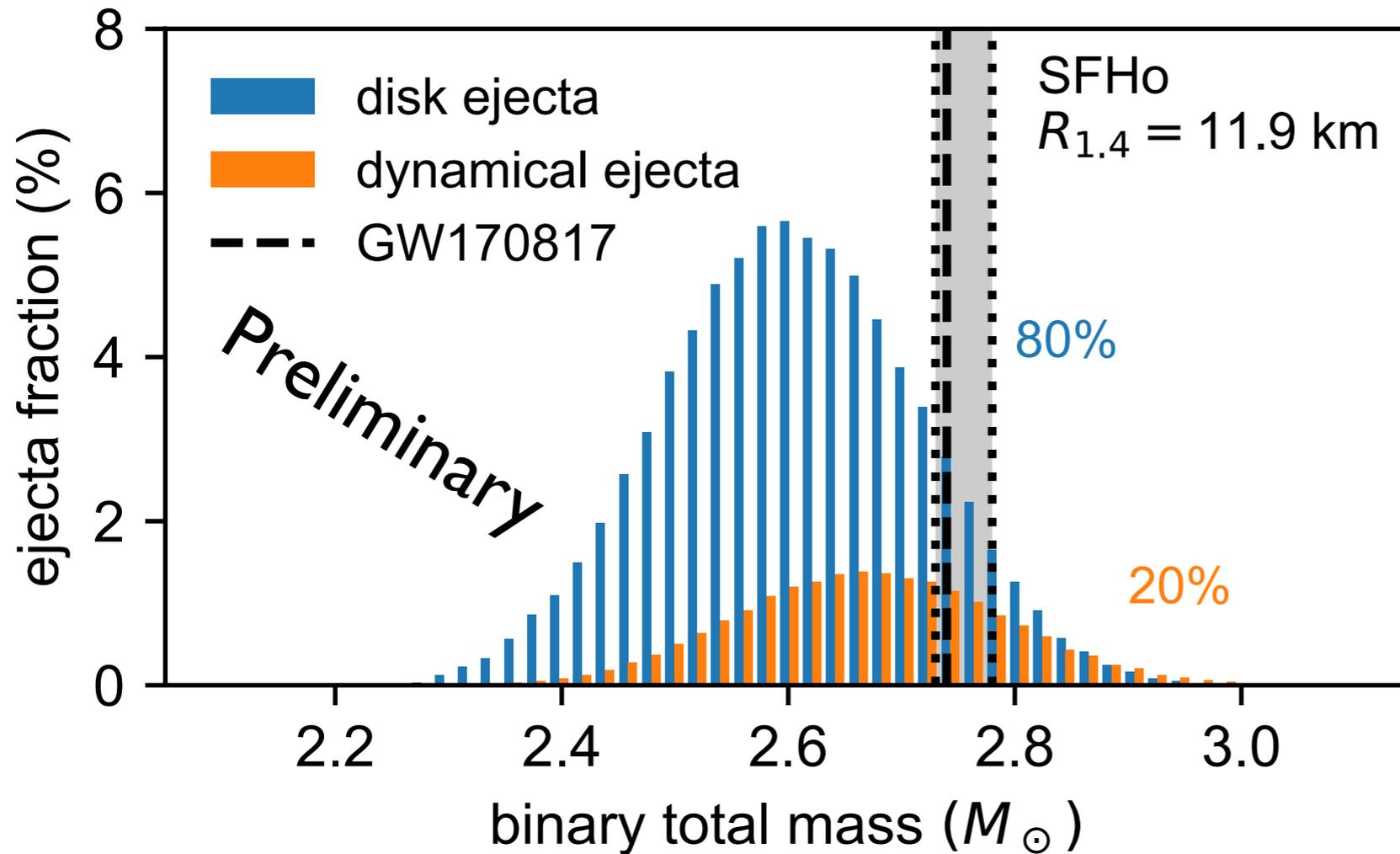
trapped, emission+absorption → mostly emission → mostly absorption →  $Y_e$  freeze out

decreasing density, temperature →

disk viscous evolution, disk radius →

# Post-merger disks: exploring BNS parameter space

Siegel 2021, Nature Rev. Phys.

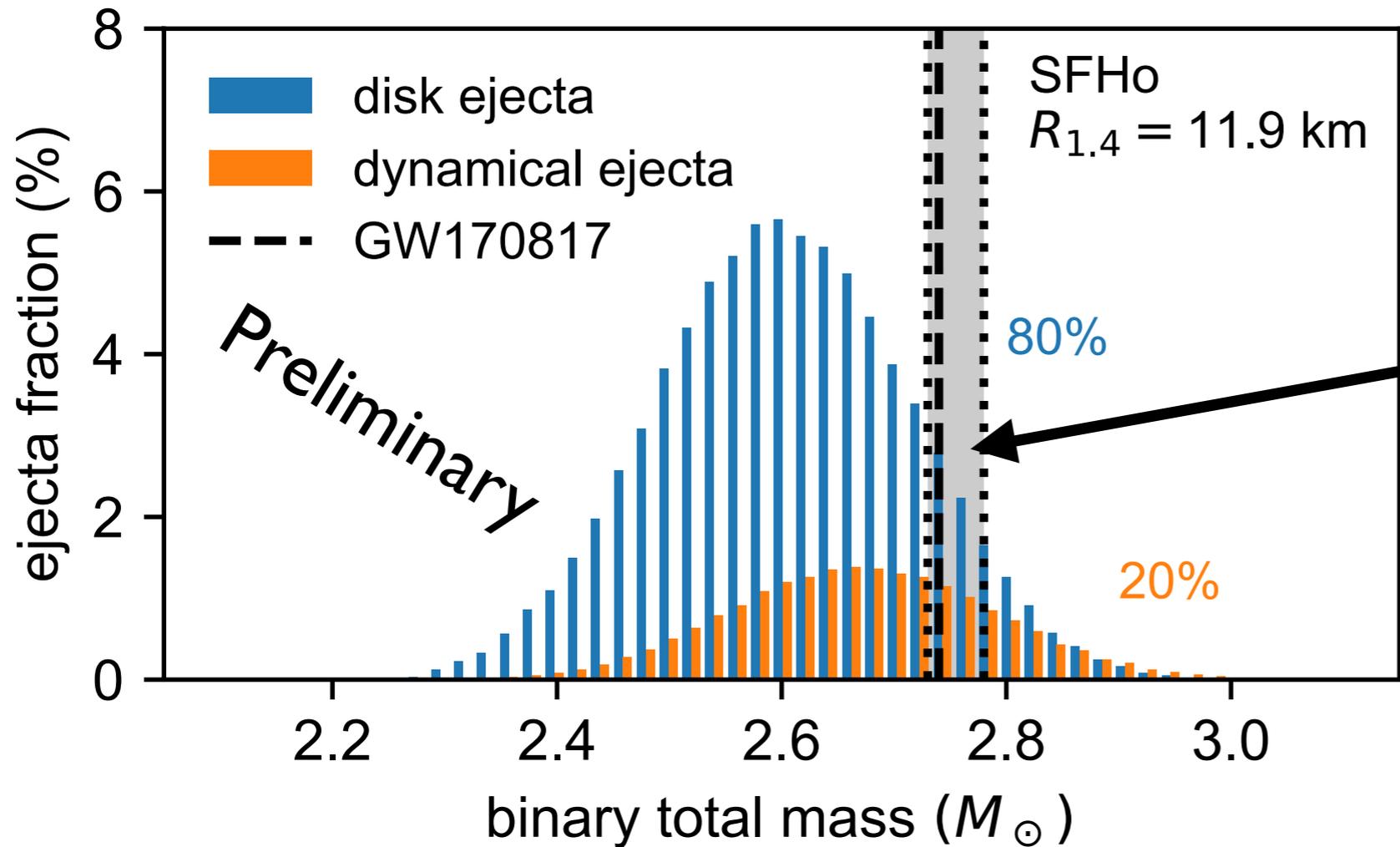


Fitting formulae: [Krüger & Foucart 2020](#)

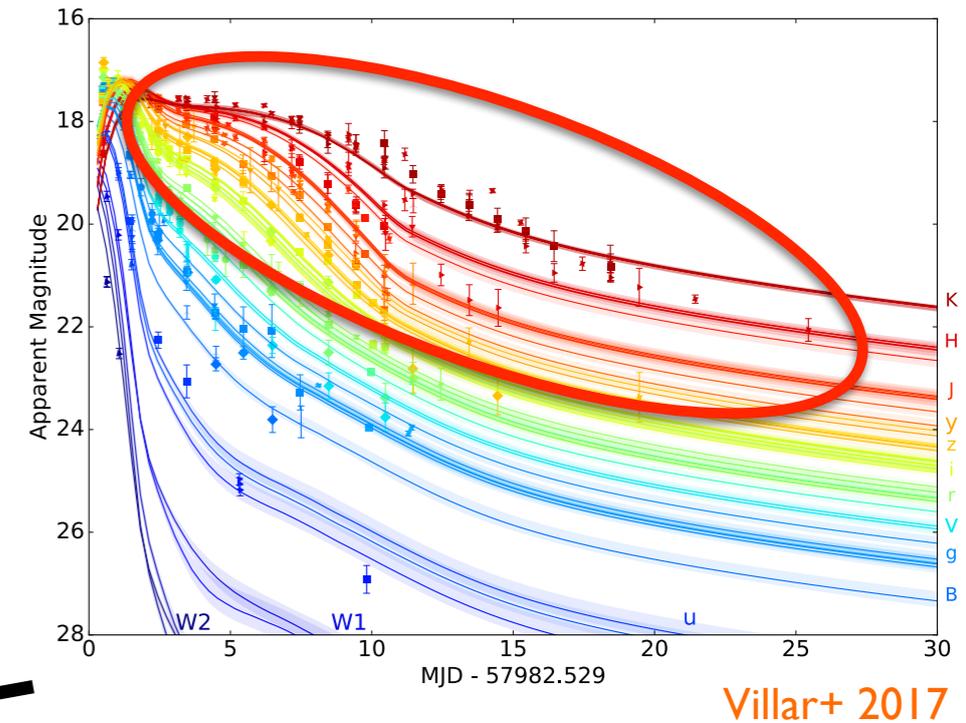
**Conjecture:** *Outflows from compact (neutrino-cooled) accretion disks synthesize most of the (heavy) r-process elements in the Universe.*

# Post-merger disks: exploring BNS parameter space

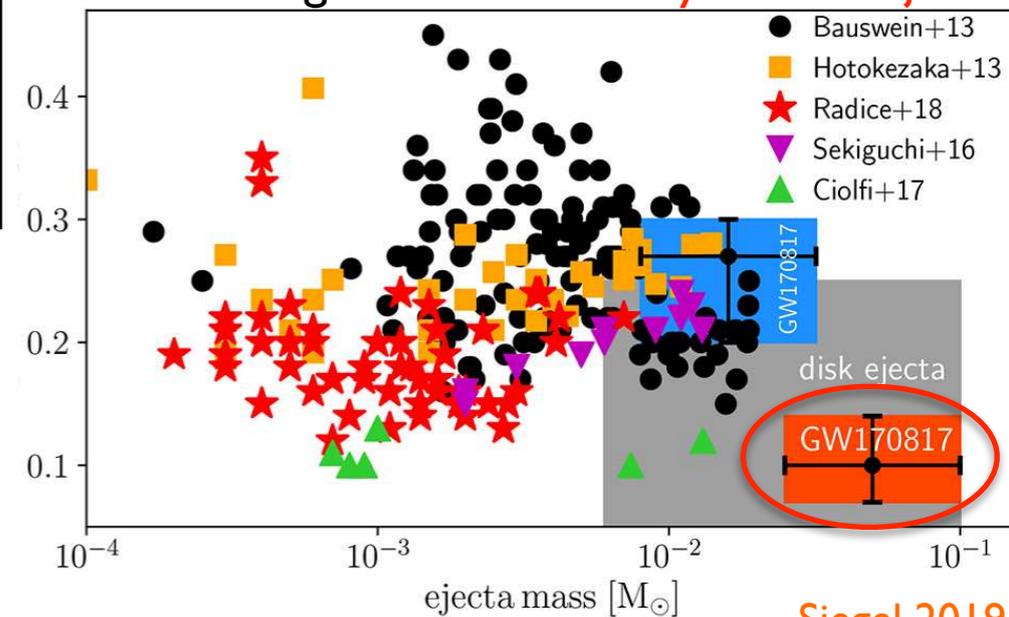
Siegel 2021, Nature Rev. Phys.



Fitting formulae: Krüger & Foucart 2020

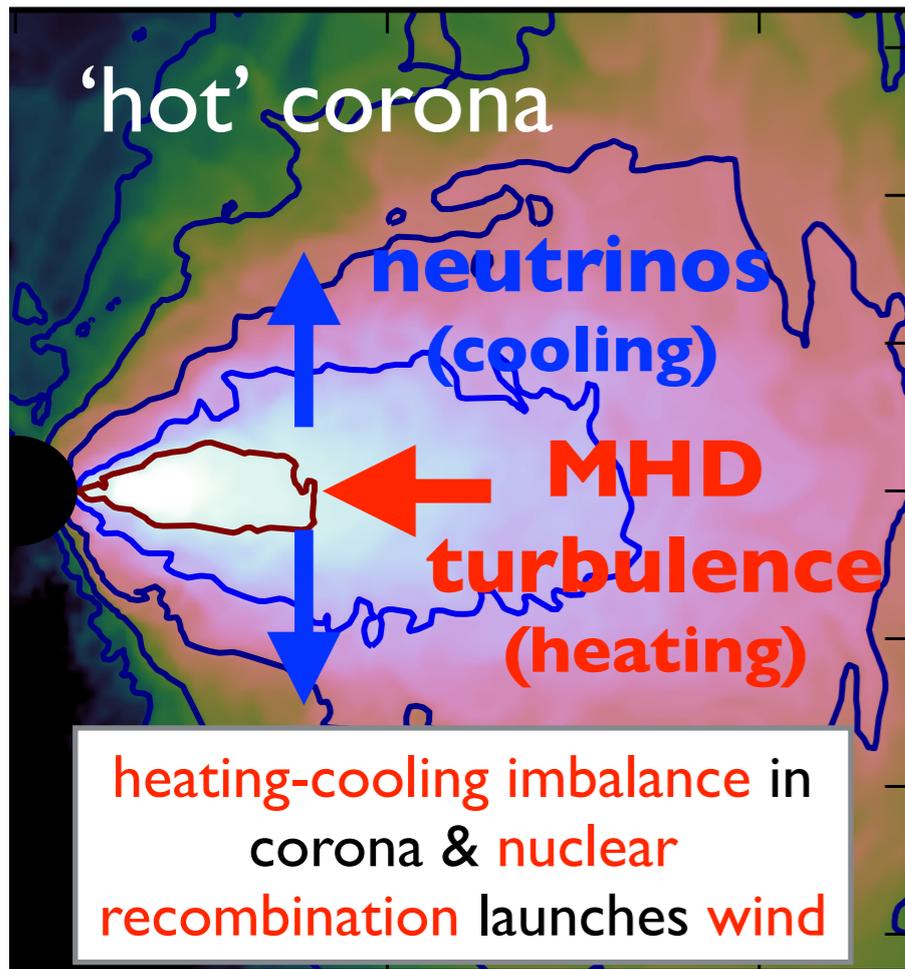


BNS merger simulations: dynamical ejecta

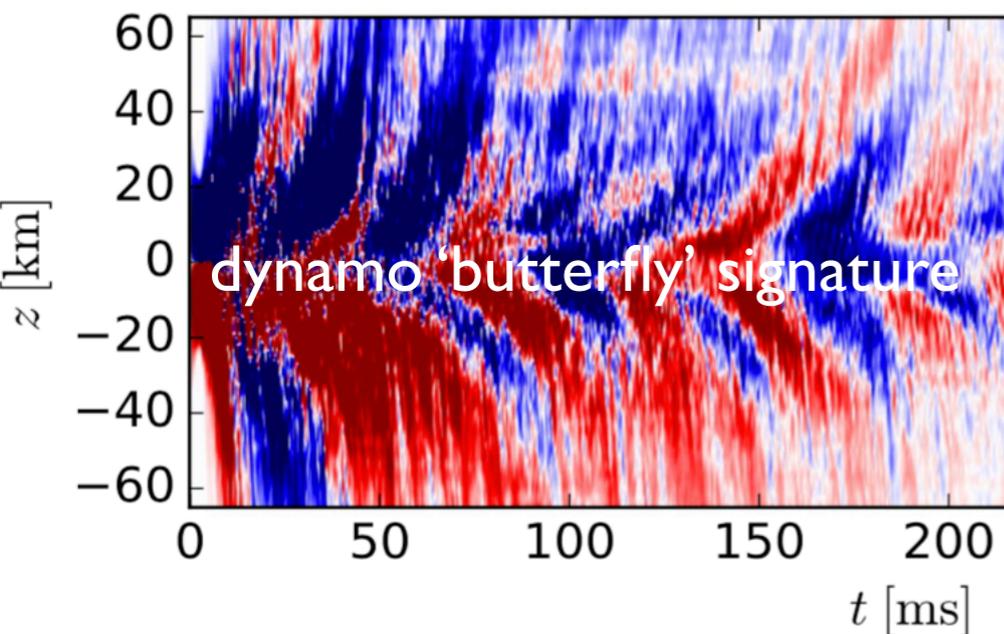


**Conjecture:** *Outflows from compact (neutrino-cooled) accretion disks synthesize most of the (heavy) r-process elements in the Universe.*

# Weak interactions in post-merger disks



Siegel & Metzger, PRL 2017



Weak interactions are key for composition, nucleosynthesis, kilonova

Importance of weak interactions:

$$\mathcal{R} = \frac{Q_{\nu}^{-}}{Q^{+}} \sim \frac{1}{2}$$

neutrino emission

viscous heating (MRI)

ID alpha-disk model

Ignition threshold:

De & Siegel 2021

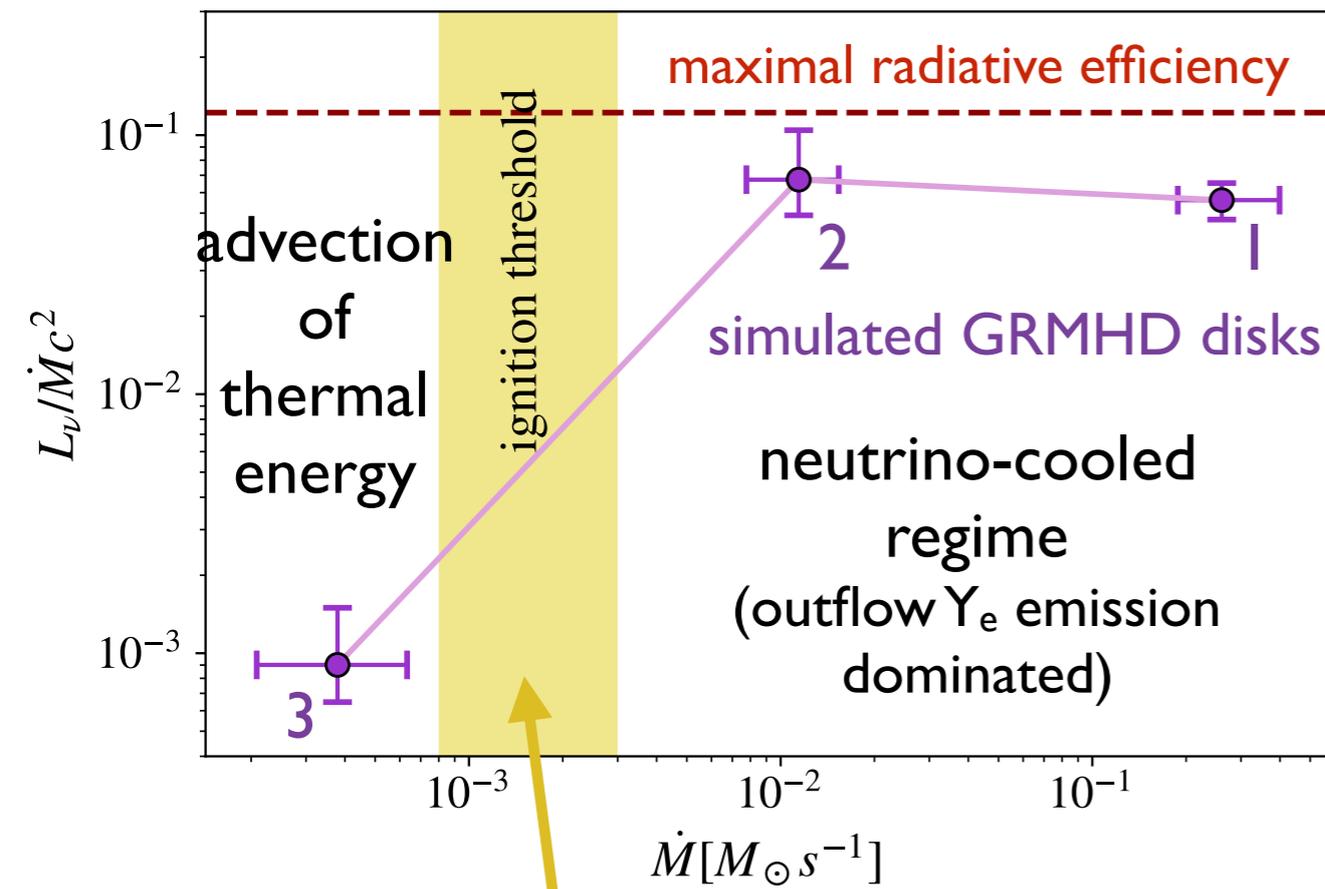
$$\dot{M}_{\text{ign}} = 2 \times 10^{-3} M_{\odot} \text{s}^{-1} \left( \frac{M_{\text{BH}}}{3M_{\odot}} \right)^{\frac{4}{3}} \left( \frac{\alpha_{\text{eff}}}{0.02} \right)^{\frac{3}{5}}$$

Accretion rate parametrizes importance of weak interactions

# Ignition of weak interactions

De & Siegel 2021

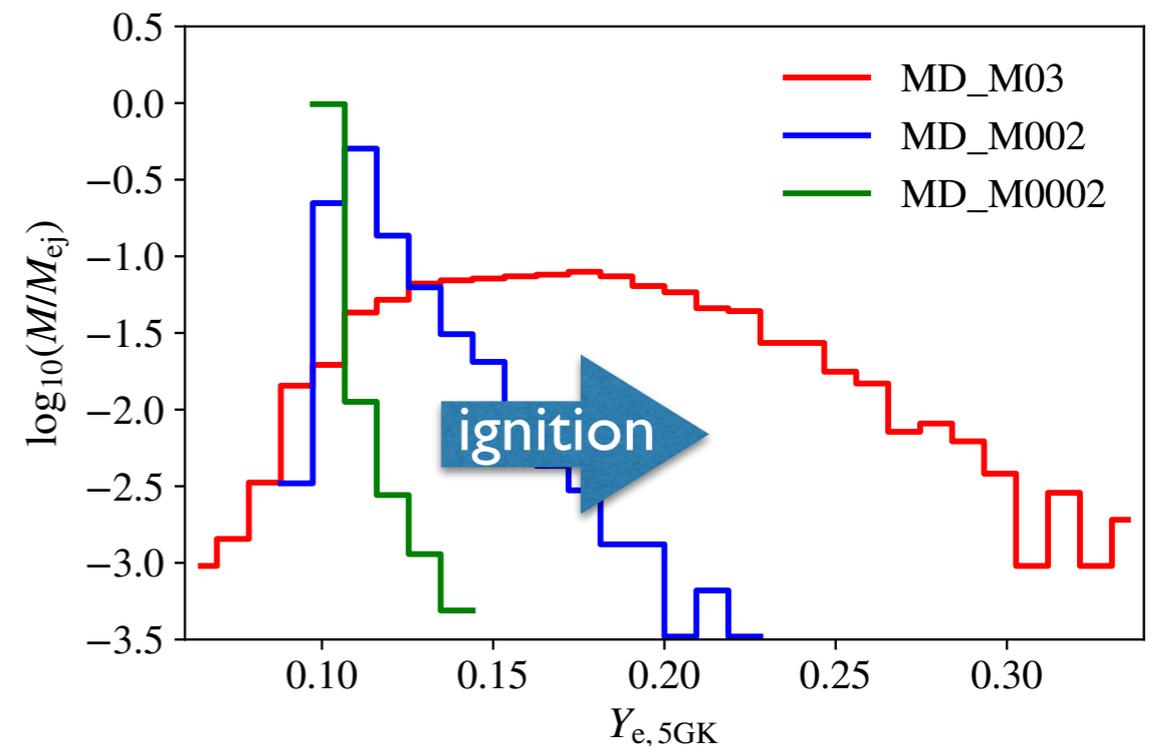
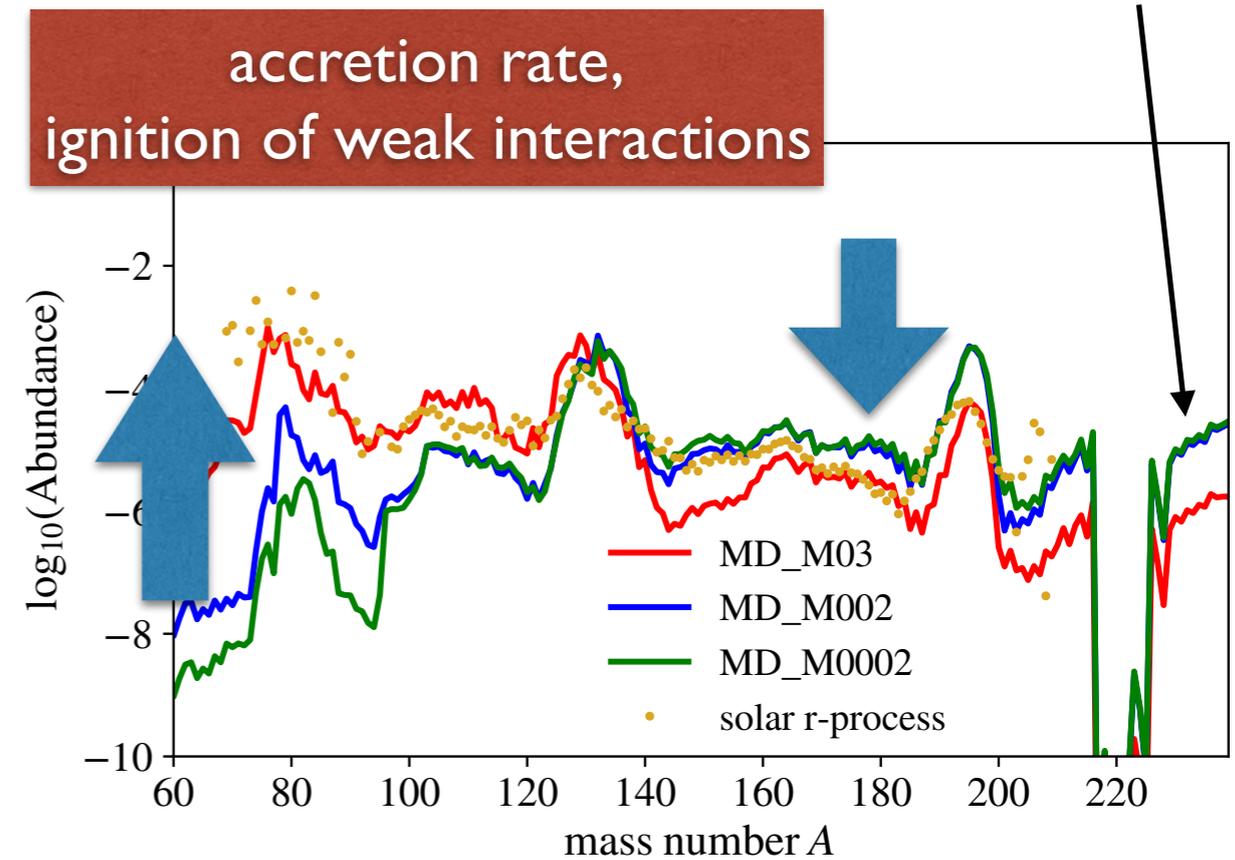
actinide abundances



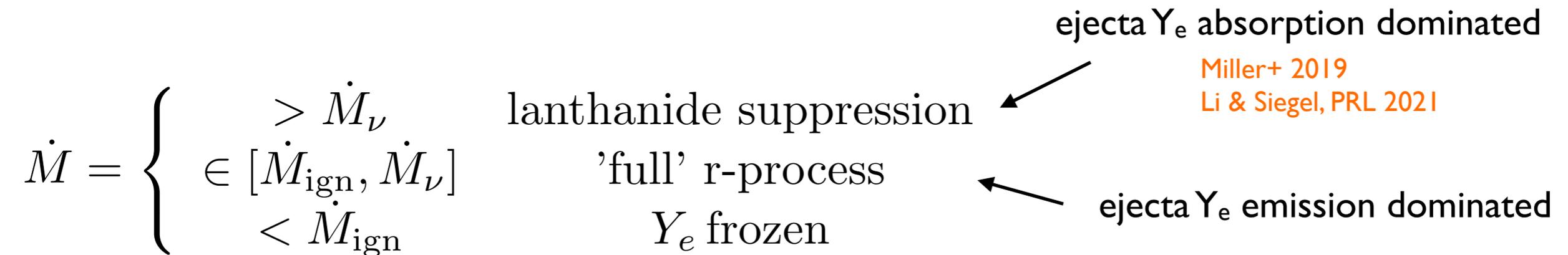
analytic estimate

Ejected disk mass:

- 1 ~ 35%
  - 2 ~ 35%
  - 3 ~ 60%
- see also:  
 Siegel & Metzger 2018  
 Fernandez+ 2019, 2020  
 Christie+ 2019
- more effective evaporation in the absence of cooling



# Nucleosynthesis regimes

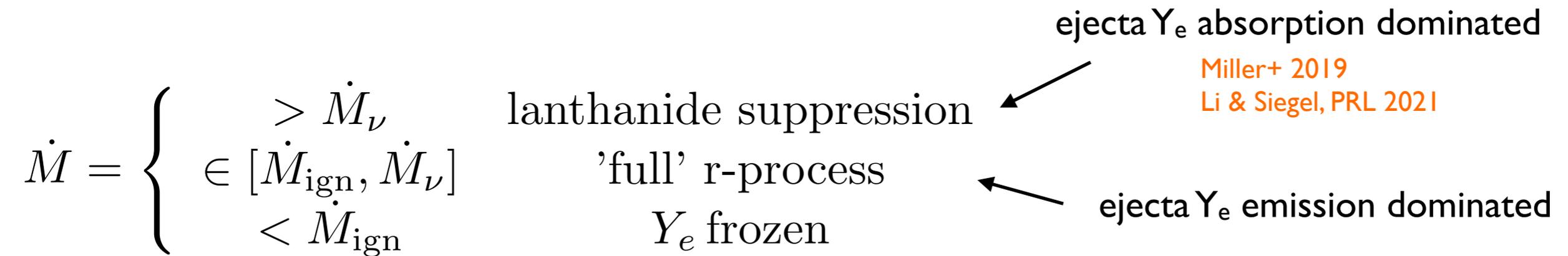


$$\dot{M}_\nu \simeq 0.1 M_\odot \text{s}^{-1} \left( \frac{M_{\text{BH}}}{3M_\odot} \right)^{\frac{4}{3}} \left( \frac{\alpha_{\text{eff}}}{0.02} \right)$$

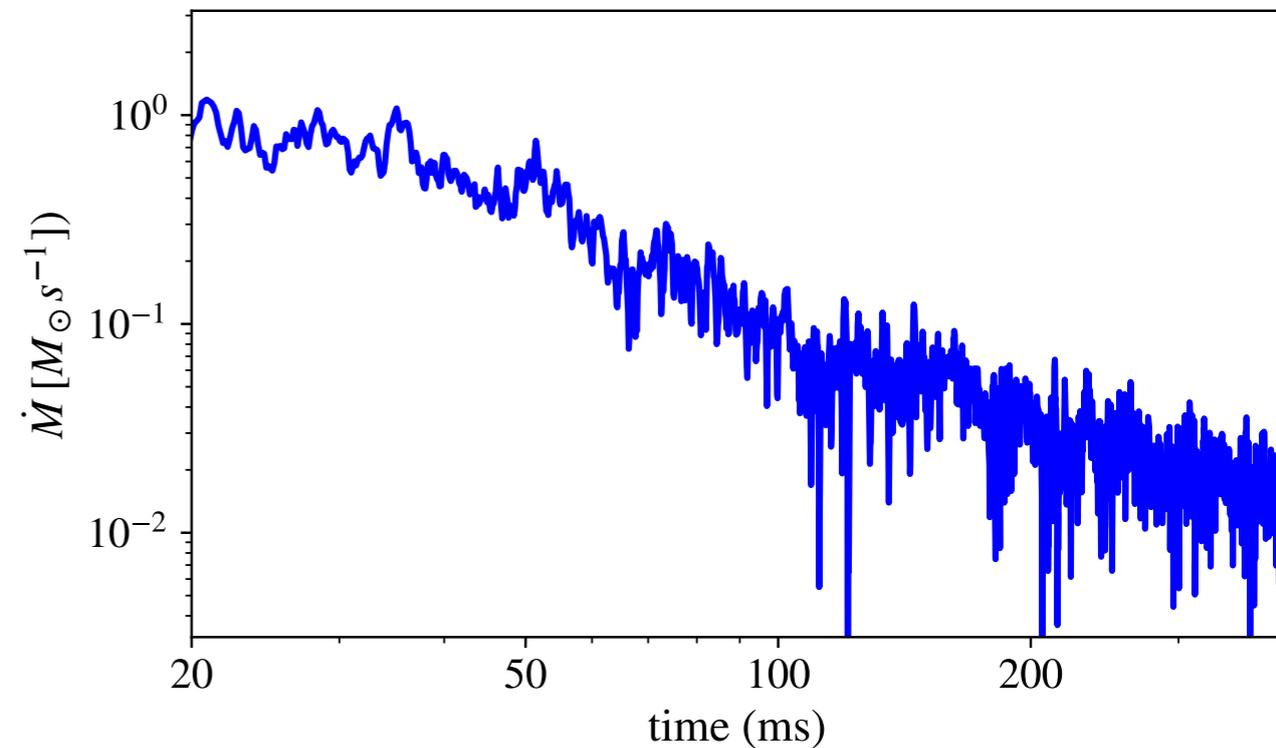
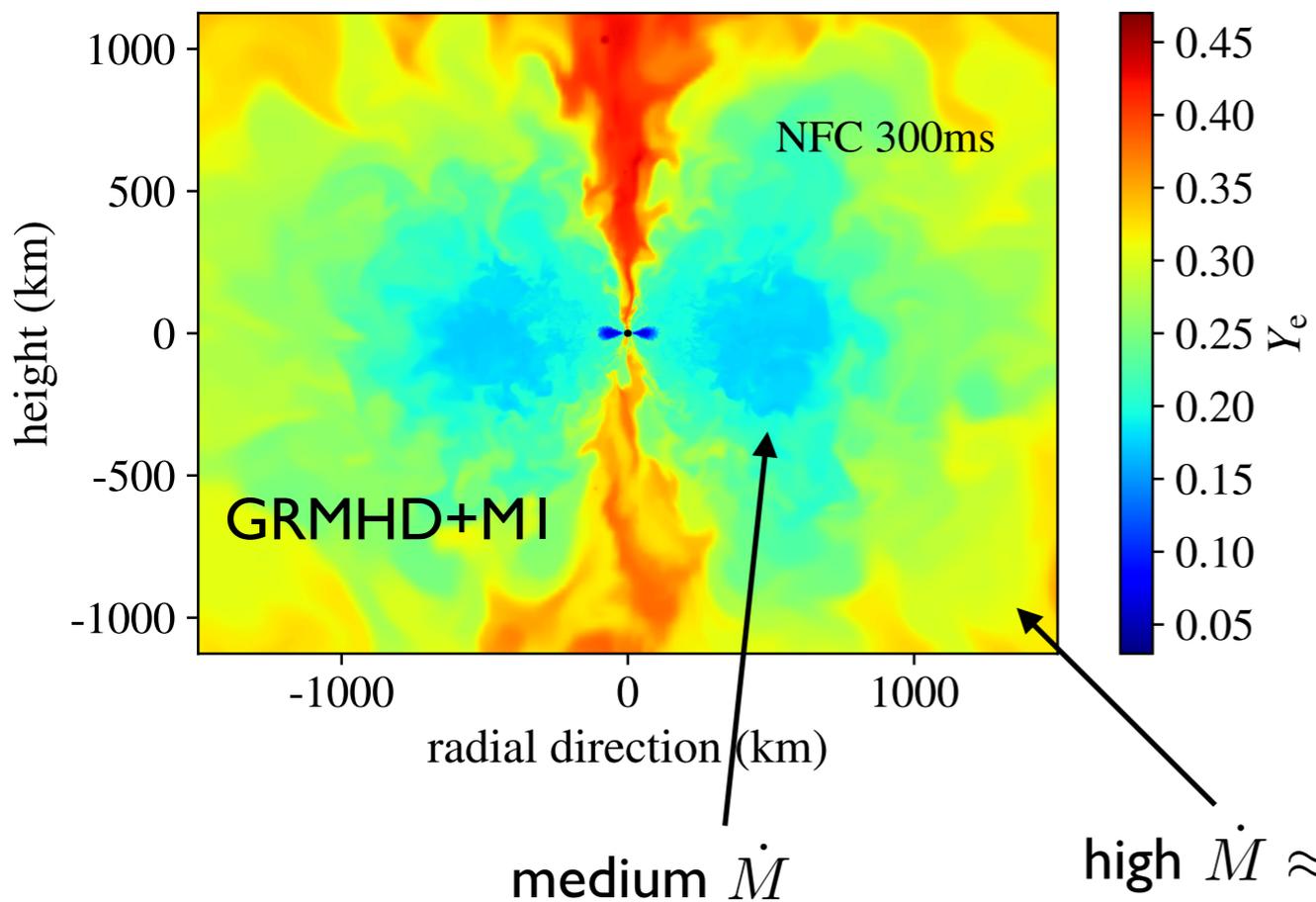
$$\dot{M}_{\text{ign}} \simeq 2 \times 10^{-3} M_\odot \text{s}^{-1} \left( \frac{M_{\text{BH}}}{3M_\odot} \right)^{\frac{4}{3}} \left( \frac{\alpha_{\text{eff}}}{0.02} \right)^{\frac{5}{3}}$$

Post-merger accretion disk can 'sweep through' one or more regimes while viscously spreading

# Nucleosynthesis regimes

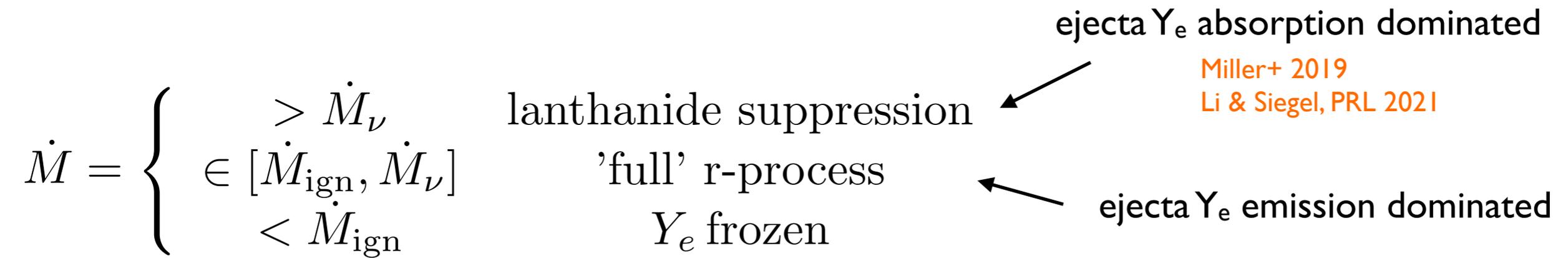


Li & Siegel, PRL 2021

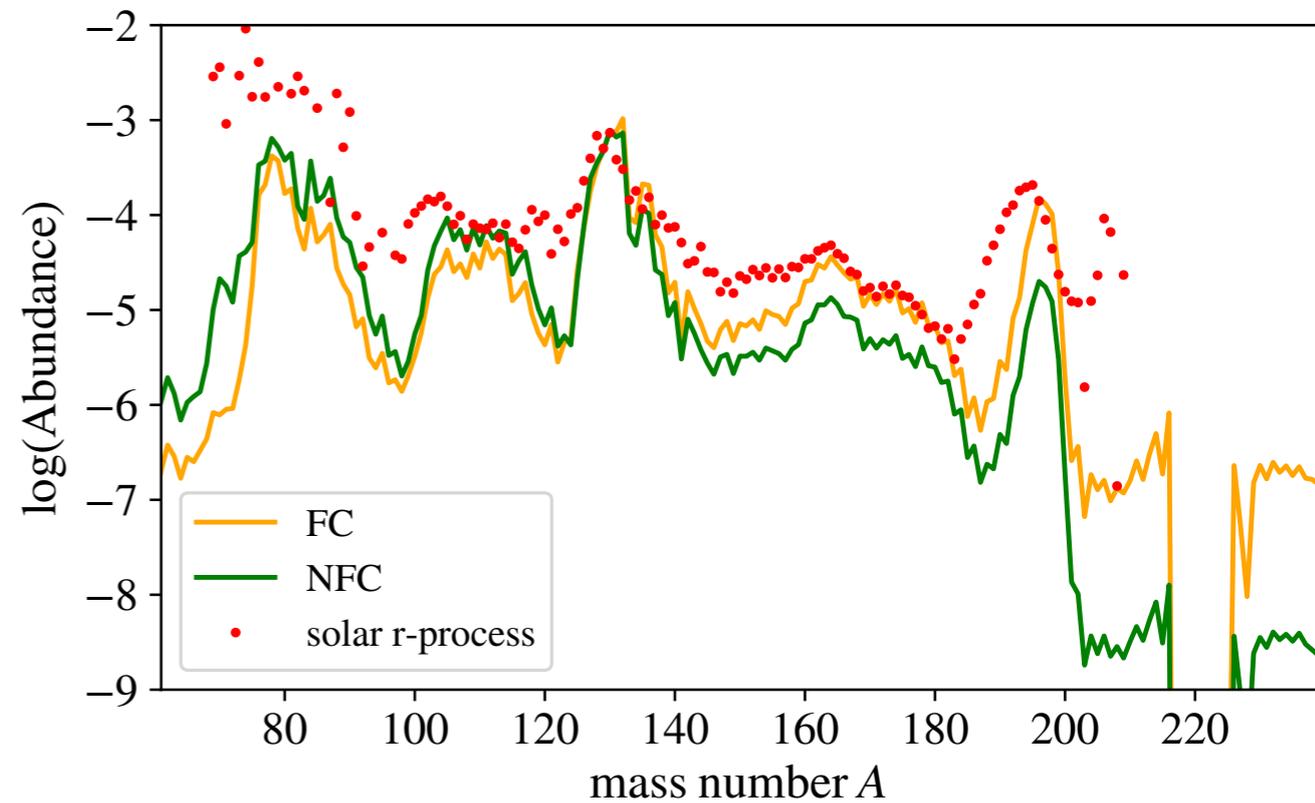
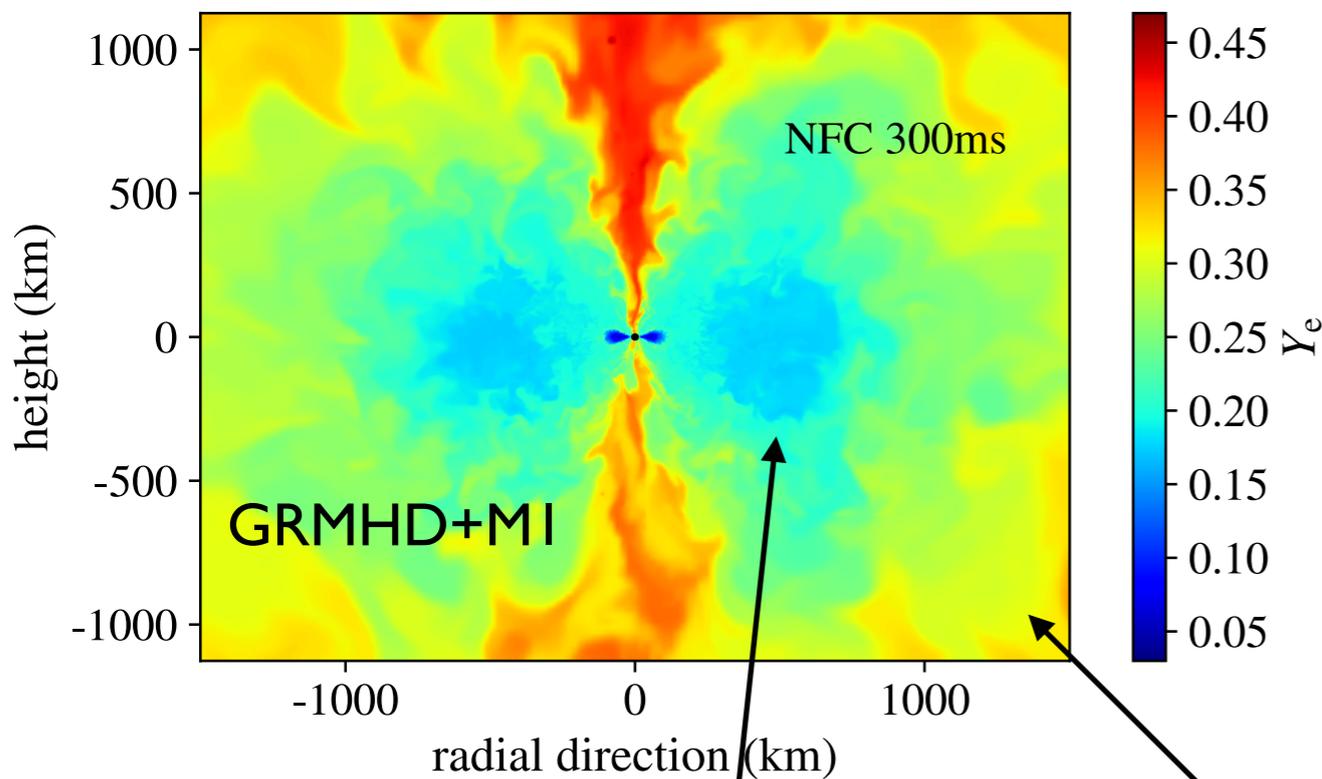


high  $\dot{M} \approx 1 M_\odot s^{-1}$

# Nucleosynthesis regimes



Li & Siegel, PRL 2021

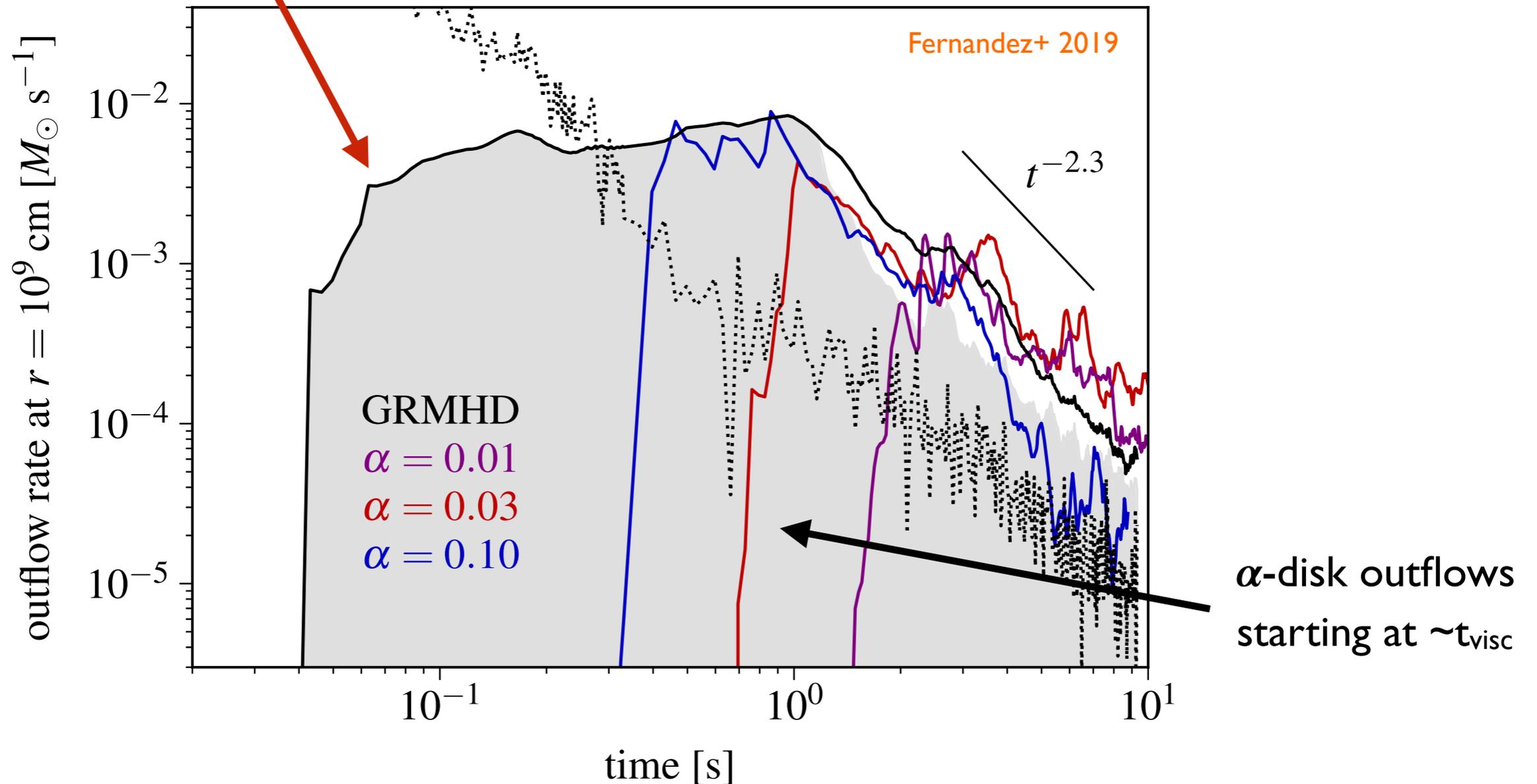


medium  $\dot{M}$

high  $\dot{M} \approx 1M_\odot \text{s}^{-1}$

# MHD vs. $\alpha$ -disks

GRMHD outflows are early!



- $\alpha$ -disks: viscous outflows, **ejected late**  $t > t_{\text{visc}}$ ,  $Y_e$  set by freeze-out in disk relative to  $t_{\text{visc}}$   
Fernandez+ 2013, 2020, Just+ 2015, 2021, Fujibayashi+ 2018, 2020
- MHD-disks: outflows arise early (heating-cooling imbalance)  $t < t_{\text{visc}}$ ,  $Y_e$  set by weak physics early on  
Siegel & Metzger 2017, 2018, Fernandez+ 2019, Miller+ 2019, Just 2021

# Neutrino fast flavour conversions

Li & Siegel 2021, PRL

Kinetic equation for neutrino transport (similar for  $\bar{\nu}$ ):

$$i v^\mu \partial_\mu \rho_\nu = [H, \rho_\nu] + \mathcal{C} \quad H = H_V + H_M + H_\nu \quad \rho_\nu = \begin{pmatrix} f_{\nu_e} & f_{\langle \nu_e | \nu_\mu \rangle} & f_{\langle \nu_e | \nu_\tau \rangle} \\ f_{\langle \nu_\mu | \nu_e \rangle} & f_{\nu_\mu} & f_{\langle \nu_\mu | \nu_\tau \rangle} \\ f_{\langle \nu_\tau | \nu_e \rangle} & f_{\langle \nu_\tau | \nu_\mu \rangle} & f_{\nu_\tau} \end{pmatrix}$$

“Collisions”: emission, absorption

$$H_V \equiv \frac{M^2}{2E}, \quad \text{vacuum oscillations}$$

$$H_M \equiv -v^\mu \Lambda_\mu \frac{\sigma_3}{2}, \quad \text{matter interaction (“MSW”)}$$

$$H_\nu \equiv -\sqrt{2} G_F \int \frac{E'^2 dE'}{2\pi^2} d\Gamma' v^\mu \boxed{v'_\mu \rho'_\nu} \quad \text{self-interaction}$$

Diagonal: usual occupation number  
Off-diagonal: flavour coherence

Flavor evolution due to off-diagonal terms in  $H$ ;  $H_\nu$  can cause run-away modes (non-linearity)

Conditions for fast conversions:

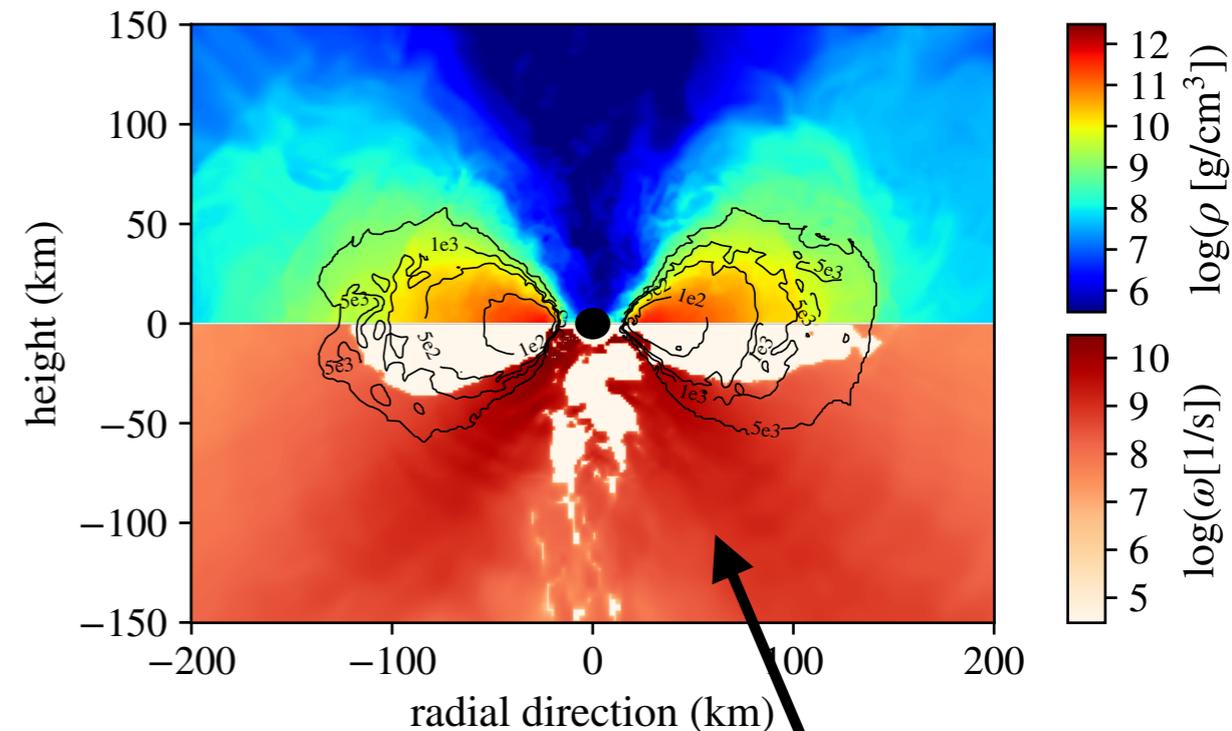
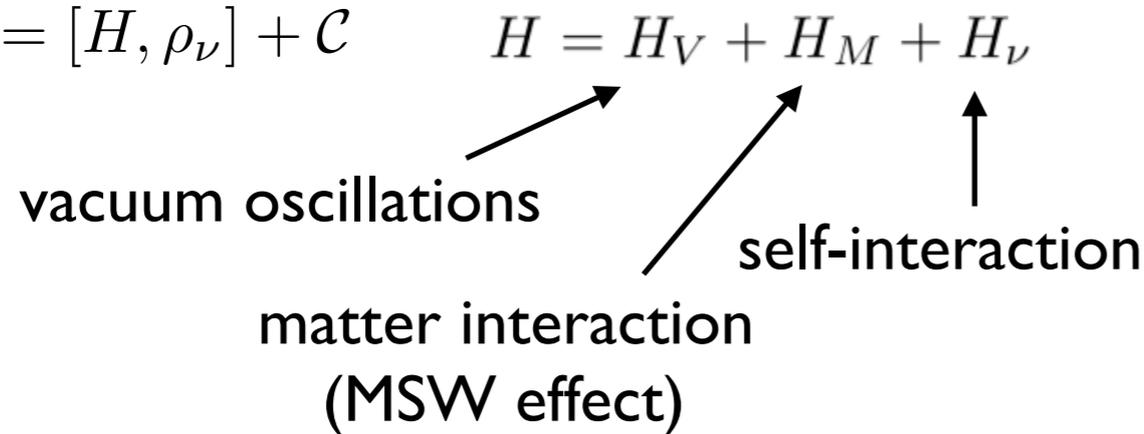
$$\Phi_0 = \sqrt{2} G_F \hbar^{-1} n_\nu = 1.92 \times 10^9 \text{s}^{-1} \left( \frac{n_\nu}{10^{31} \text{cm}^{-3}} \right)$$

# Neutrino oscillations in post-merger disks

Li & Siegel 2021, PRL

Kinetic equation for neutrino transport:

$$i v^\mu \partial_\mu \rho_\nu = [H, \rho_\nu] + \mathcal{C}$$



ubiquitous flavor conversions  
~ns timescales

- GRMHD + MI neutrino radiation transport
- First simulation with fast conversions included dynamically [Wu+ 2017](#) [George+ 2020](#)
- Dispersion relation approach [Izaguirre+ 2017](#)
- Use equivalence principle in GRMHD+MI formalism to compute dispersion relation locally
- Outcome of non-linear regime of instability still uncertain, assume approximate equipartition [Richers+ 2021](#)

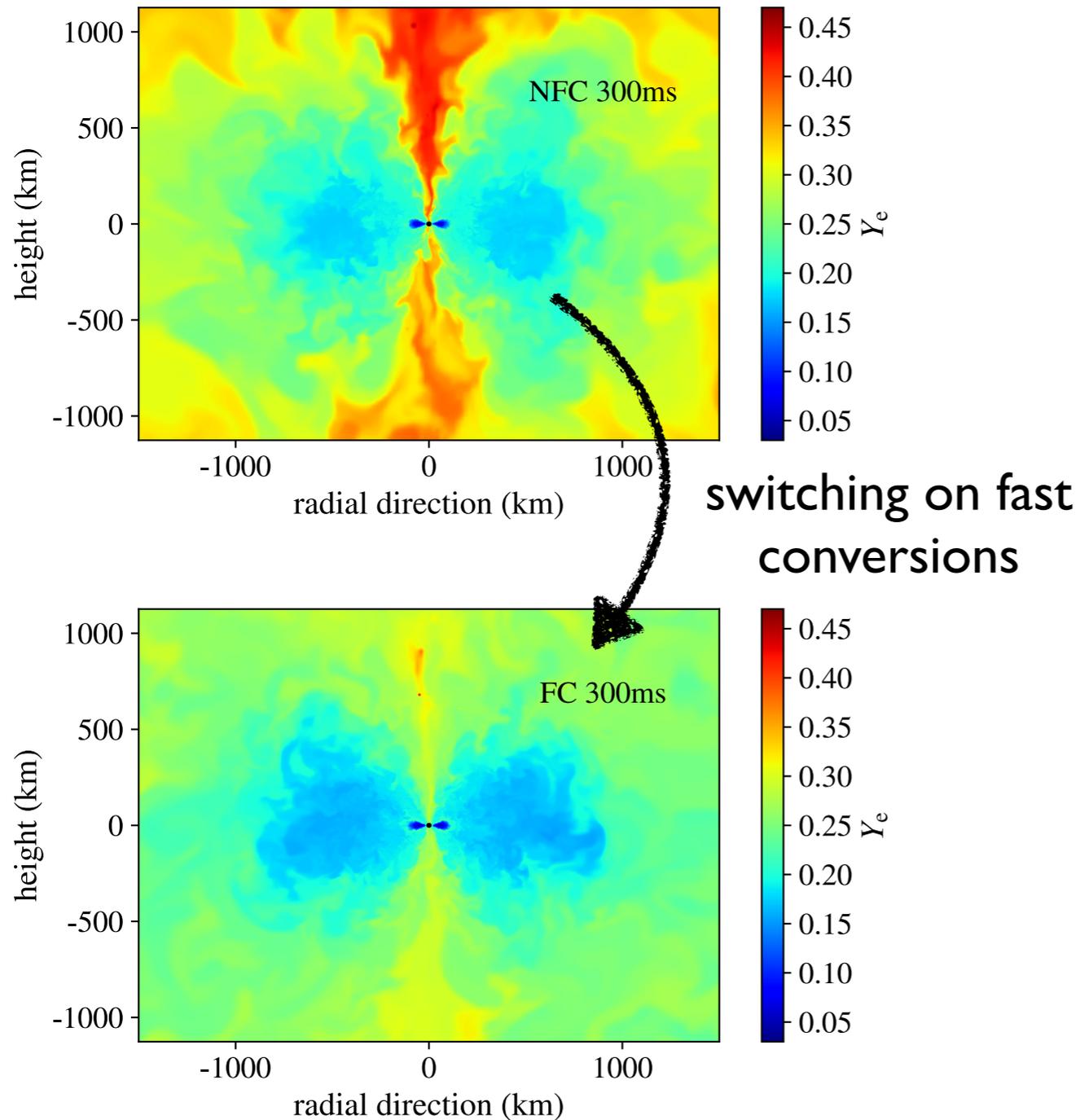
First astrophysical simulation with fast conversions,

also relevant to core-collapse supernovae

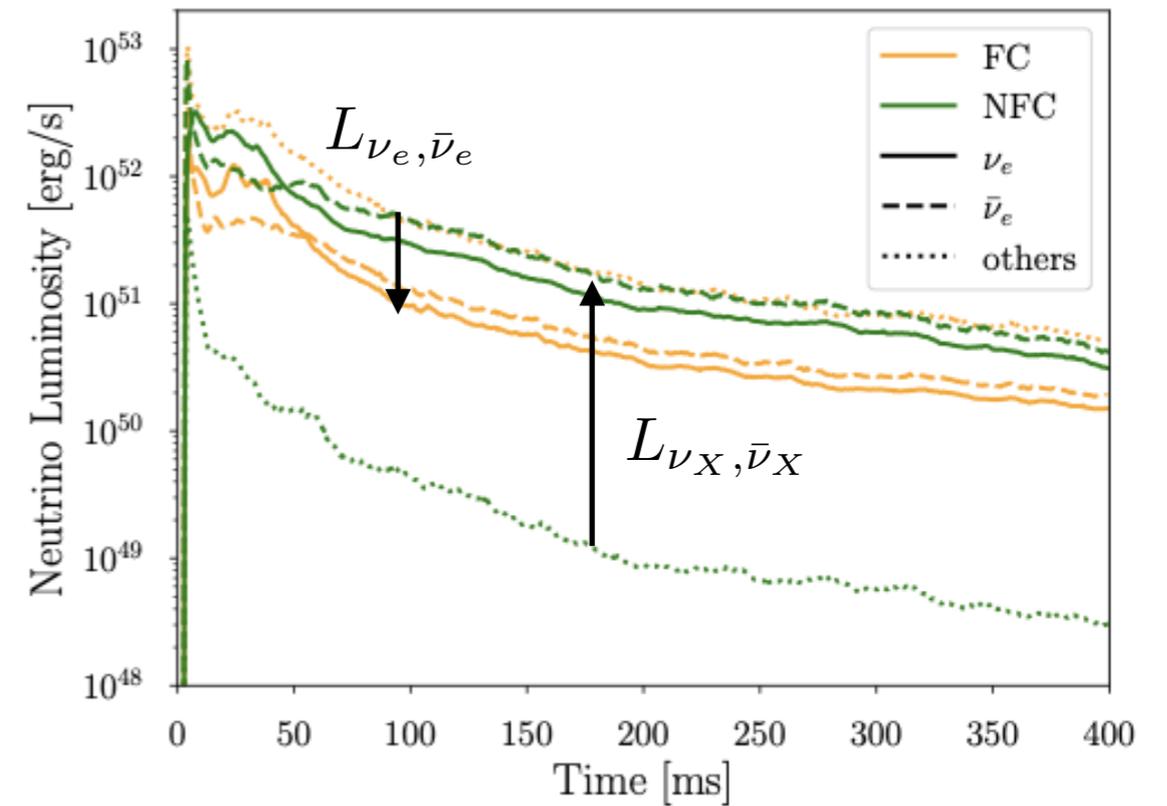
[Nagakura+ 2019](#)

# Neutrinos & r-process: fast flavour conversions

Li & Siegel 2021, PRL

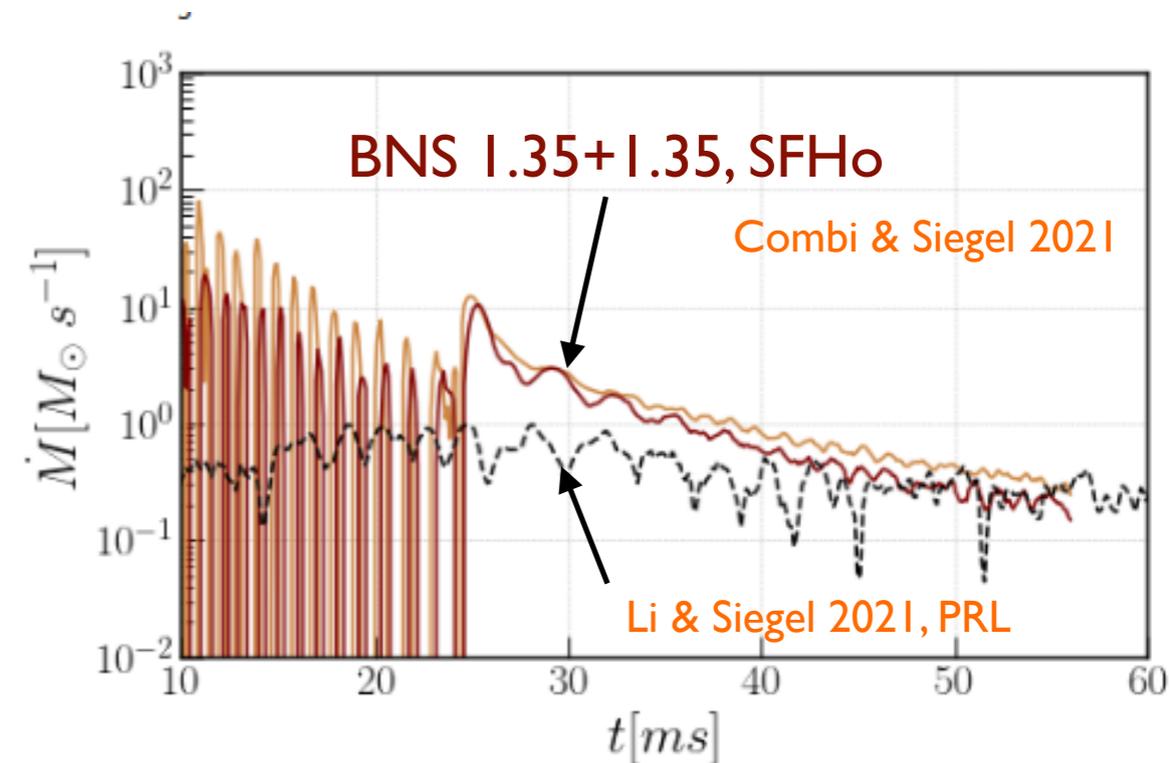
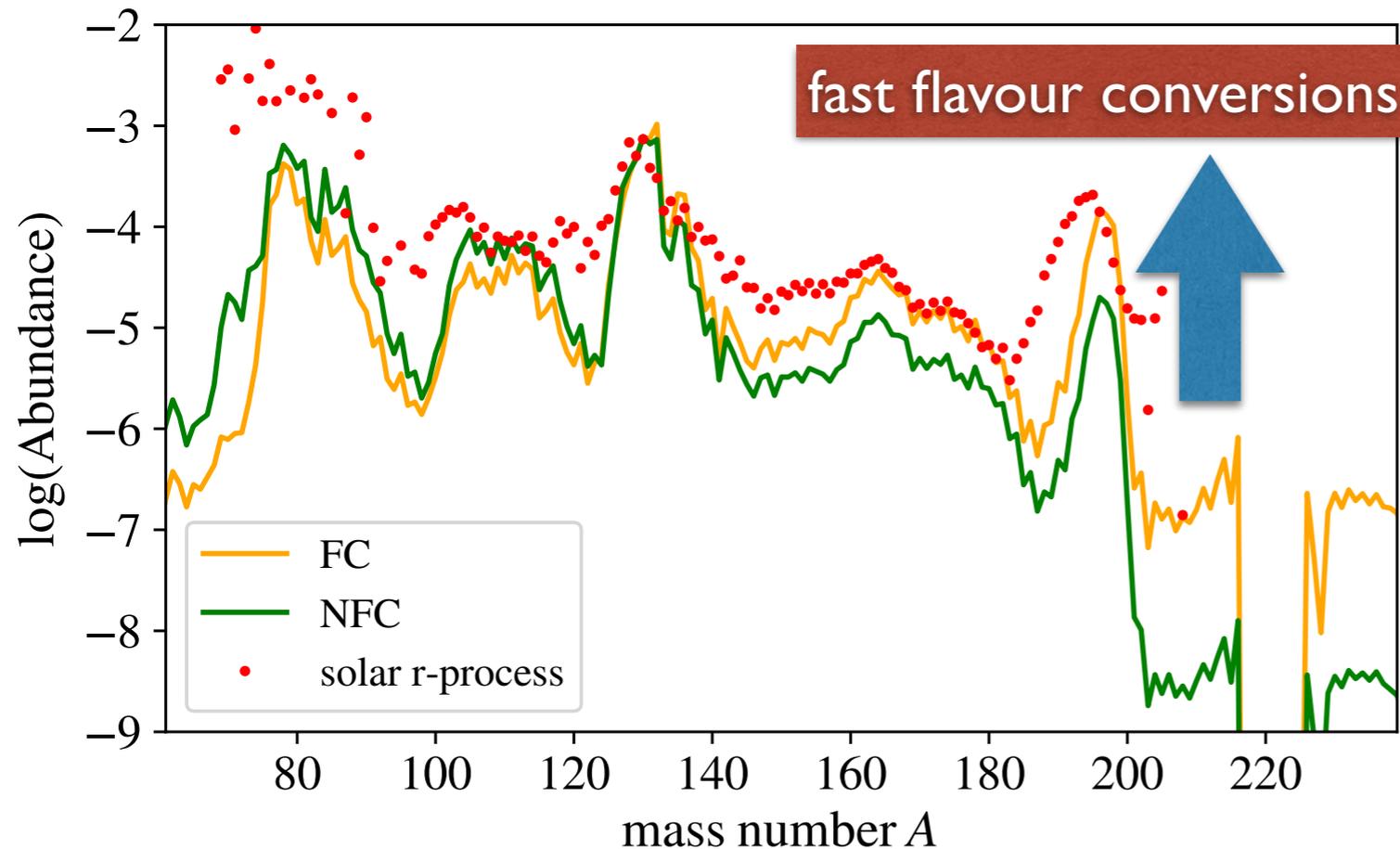


ejecta becomes more neutron rich



# Neutrinos & r-process: fast flavour conversions

Li & Siegel 2021, PRL



- boost **lanthanide** mass fraction by **factor ~2-few**
- boost **3rd peak** r-process elements by **factor ~10**

➔ can convert a kilonova from 'blue' to 'red'

➔ massive disks ( $\dot{M} \sim 1M_{\odot} s^{-1}$ ) can produce heavy r-process similar to solar

# Conclusions

- NS mergers give rise to various ejecta components with a broad range of properties
  - multi-component kilonovae, relative strength determined by binary parameters
  - ejecta expected to be dominated by disk outflows
  - much of post-merger phenomenology still poorly understood
- post-merger BH-accretion disk parameter space mostly determined by single parameter: accretion rate
  - various nucleosynthesis regimes
  - GRMHD & 3D crucial for nature of outflows, composition, r-process, kilonovae
- first simulations with neutrino fast flavour conversions suggest observable imprint: boost in heavy elements and opacity
  - red kilonova possible even for very massive disks
  - r-process abundances can be similar to solar
  - also important for early post-merger phase, much to be explored